

**A Panel Data Approach for Program Evaluation — Measuring  
the Benefits of Political and Economic  
Integration of Hong Kong with Mainland China\***

by

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Abstract

We propose a simple to implement panel data method to evaluate the impacts of social policy. The basic idea is to exploit the dependence among cross-sectional units to construct the counterfactuals. The cross-sectional correlations are attributed to the presence of some (unobserved) common factors. However, instead of trying to estimate the unobserved factors, we propose to use observed data. We use a panel of 24 countries to evaluate the impact of political and economic integration of Hong Kong (HK) with Mainland China. We find that the political integration hardly had any impact on the growth of the Hong Kong economy. However, the economic integration has raised HK's annual real GDP by about 4%.

Keywords: panel data, factor model, cross-sectional dependence, program evaluation, ARMA models.

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## 1. Introduction

This paper proposes a panel data methodology to measure the impact of political and economic integration of Hong Kong with China. One of the difficulties of using nonexperimental data to measure the economic impact of a policy intervention is not being able to simultaneously observe the outcomes of an entity under the intervention and not under the intervention (e.g. Heckman and Hotz (1989), Rosenbaum and Rubin (1983)). Panel data with observations for a number of individuals over time will often contain information on some individuals that are subject to policy intervention and some that are not. If the reactions of individuals towards policy changes are similar (e.g. Hsiao (2003), Hsiao and Tahmiscioglu (1997)) or even if their responses are different, as long as they are driven by some common factors (e.g. Gregory and Head (1999), Sargent and Sims (1977)), information on other individuals not subject to policy intervention can help to construct the counterfactuals of those who are subject to policy changes.

Hong Kong was a fishing village ceded to Britain after the opium war in 1842. Many Mainland Chinese migrated to Hong Kong after the establishment of the People's Republic of China in 1949. The population at 1950 was about 2.6 million. In the 1960's and 1970's Hong Kong experienced rapid economic growth and is now considered one of the four "little dragons" in East Asia. In 1961, its per capita income was US\$410, about 13.8 percent of that of the United States. By the eve of reverting sovereignty back to China on July 1, 1997, Hong Kong's population was 6.5 million with per capita income of US\$21,441, which was 67.2 percent of that of the U.S.<sup>1</sup> The Hang Seng stock market index was at 15,196. Because Hong Kong had been growing rapidly prior to the reversion of sovereignty to China, many questions have been raised about the impacts of the change of sovereignty on the growth of the Hong Kong economy (e.g. Sung and Wong (2000)). As a matter of fact, on the eve of Hong Kong's signing of the Closer Economic Partnership Arrangement (CEPA) with Mainland China in June 2003, the growth rate for the second quarter of 2003

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<sup>1</sup>Hong Kong Census and Statistics Department web site, URL:<http://www.censtad.gov.hk>

was -.67 percent. The per capita income was US\$22,673 in 2003. The Hang Seng Index fell to 8717 in April 2003.

The CEPA aimed to strengthen the linkage between Mainland China and Hong Kong by liberalizing trade in services, enhancing cooperation in the area of finance, promoting trade and investment facilitation and mutual recognition of professional qualifications. The implementation of CEPA started on January 1, 2004 when 273 types of Hong Kong products could be exported to the Mainland tariff free, another 713 types were added on January 1, 2005, 261 on January 1, 2006, and a further 37 on January 2007. Chinese citizens residing in selected cities were also allowed to visit Hong Kong as individual tourists, from 4 cities in 2003 to 49 cities in 2007, including all 21 cities in Guangdong province.

In this paper we try to assess the impact of the political and economic integration of Hong Kong with Mainland China on Hong Kong's economy by comparing what actually happened to Hong Kong's real GDP growth rates with what would have happened if there had been no change of sovereignty in July 1997 or no CEPA with Mainland China in 2003. More specifically, we wish to analyze how these events have changed the growth rate of Hong Kong. However, to answer this question through conventional econometric modelling is not easy. We need to know how and why the Hong Kong economy has grown over time and how the China factor plays a role in Hong Kong's investment, labor migration and Hong Kong as an entrepot between China and the rest of the world, etc. Most of the growth literature is highly abstract. Empirical analysis based on the theoretical literature would often require the imposition, as Sims (1980) claimed, of "incredible" a priori identifying restrictions. Data demand will also be huge. Moreover, often when external conditions change, people's optimal decision rules also change. There simply may not be enough post-change observations to provide reliable inferences for the post-change outcomes. In addition, Hong Kong's economy has also been subject to many external shocks after the reversion of sovereignty. The Asian financial crisis broke out in October, 1997. The Thai Baht/US dollar exchange rate was 27 in June, 1997. It fell to 35.8 in September, 1997

and further, to 44.4 Baht to U.S.\$1 in December. The crisis in Thailand quickly spread to S. Korea, Malaysia, Indonesia, Philippines, Singapore, Taiwan, and other Pacific Rim countries with varying degrees of severity. Hong Kong was hit by international speculative attacks on four occasions in 1998. H5N1 Avian flu also broke out in December 1997 that caused 5 deaths and led to the slaughtering of more than a million chickens. By December 1997, the Hang Seng index had fallen to the 10722. In March 2003 Severe Acute Respiratory Syndrome (SARS) spread to Hong Kong from China.<sup>2</sup>

If we know the outcomes of a subject under intervention and not under intervention, the effect of a policy intervention is just the difference between the outcomes under intervention and in the absence of intervention. However, we rarely simultaneously observe the outcomes of an individual under intervention or in the absence of intervention. To properly evaluate the effect of a policy intervention on a subject or unit we need to construct the counterfactuals of the missing outcomes. Our approach to constructing the counterfactuals of the individual subject to intervention, say the  $i$ th unit, is to use other units that are not subject to intervention to predict what would have happened to the  $i$ th unit had it not been subject to policy intervention. The basic idea behind this approach is to rely on the correlations among cross-sectional units. We attribute the cross-sectional dependence to the presence of common factors that drive all the relevant cross-sectional units. In section 2 we set up the basic model. Section 3 proposes a panel approach to construct the counterfactuals without the need to identify the underlying model. Section 4 discusses a procedure to evaluate the time-varying treatment effects of a social program. Section 5 discusses strategies for selecting the most relevant cross-sectional units to construct counterfactuals. Section 6 discusses the data sources. Empirical results are presented in section 7. Conclusions are in section 8.

## 2. The Basic Model

The basic approach for constructing the counterfactuals is to rely on the correlations

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<sup>2</sup>For more information, see Jao (2001).

among cross-sectional units. We assume the correlations among cross-sectional units are due to some common factors that drive all cross-sectional units, although their impacts on each cross-sectional unit may be different. Let  $y_{it}^0$  denote the outcome of the  $i$ th unit at time  $t$  without policy intervention. As in Forni and Reichlin (1998), Gregory and Head (1999), etc. we assume that  $y_{it}^0$  is generated by a factor model of the form,

$$y_{it}^0 = \underline{b}_i' \underline{f}_t + \alpha_i + \epsilon_{it}, \quad i = 1, \dots, N, t = 1, \dots, T, \quad (2.1)$$

where  $\underline{f}_t$  denotes the  $K \times 1$  (unobserved) common factors that vary over time,  $\underline{b}_i'$  denotes the  $1 \times K$  vector of constants that may vary across  $i$ ,  $\alpha_i$  denotes the fixed individual-specific effects,  $\epsilon_{it}$  denotes the  $i$ th unit random idiosyncratic component with  $E(\epsilon_{it}) = 0$ .

Stacking  $N \times 1$   $y_{it}^0$  into a vector yields

$$\underline{y}_t^0 = B \underline{f}_t + \underline{\alpha} + \underline{\epsilon}_t, \quad (2.2)$$

where  $\underline{y}_t^0 = (y_{1t}^0, \dots, y_{Nt}^0)'$ ,  $\underline{\alpha} = (\alpha_1, \dots, \alpha_N)'$ ,  $\underline{\epsilon}_t = (\epsilon_{1t}, \dots, \epsilon_{Nt})'$ , and  $B$  is the  $N \times K$  factor loading matrix  $B = (\underline{b}_1, \dots, \underline{b}_N)'$ . We assume that

Assumption 1:  $\|\underline{b}_i\| = c < \infty$  for all  $i$ .

Assumption 2:  $\underline{\epsilon}_t$  is  $I(0)$  with  $E(\underline{\epsilon}_t) = \underline{0}$  and  $E(\underline{\epsilon}_t \underline{\epsilon}_t') = V$ , where  $V$  is a diagonal constant matrix.

Assumption 3:  $E \underline{\epsilon}_t \underline{f}_t' = \underline{0}$ .

Assumption 4:  $\text{rank}(B) = K$ .

**Remark 2.1:** Model (2.1) assumes that the individual outcome is the sum of two components, a component of a function of some common time varying factors  $\underline{f}_t$  that drive all cross-sectional units and an idiosyncratic component consists of a function of individual specific effects  $\alpha_i$  and a random component  $\epsilon_{it}$ . We assume the idiosyncratic components are uncorrelated across individuals.<sup>3</sup> The correlation across individuals are caused by the

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<sup>3</sup>As pointed out by a referee that the assumption about the idiosyncratic components being mutually uncorrelated rules out the possibility of local dependence. Although a distinction

common factors,  $\underline{f}_t$ . However, the impact of common factors  $\underline{f}_t$  on individuals can be heterogeneous by allowing  $\underline{b}_i \neq \underline{b}_j$ .

**Remark 2.2:** We made no assumption about the time series properties of  $\underline{f}_t$ . It can be nonstationary or it can be stationary with  $\lim_{T \rightarrow \infty} \frac{1}{T} \sum_{t=1}^T \|\underline{f}_t\|^2 = \text{constant}$ .

**Remark 2.3:** Assumption 4 implies that the number of observable cross-sectional units,  $N$ , is greater than the number of common time-varying factors,  $\underline{f}_t$ . The assumption is reasonable since it has been shown empirically by Sargent and Sims (1977), Giannone, Reichlin and Sala (2005) (see also Watson’s discussion of that paper in the same volume), Stock and Watson (2005) and Onatski (2009) that only a few common factors explain the bulk of the variance of macroeconomic data.

### 3. A Panel Approach to Construct Counterfactuals

Let  $y_{it}^1$  denote the outcome of the  $i$ th unit at time  $t$  under treatment or intervention and  $y_{it}^0$  denote the outcome of the  $i$ th unit in the absence of treatment or intervention at time  $t$ . Then the treatment effect for the  $i$ th unit at time  $t$  is

$$\Delta_{it} = y_{it}^1 - y_{it}^0. \quad (3.1)$$

However, often we do not simultaneously observe  $y_{it}^0$  and  $y_{it}^1$ . The observed data,  $y_{it}$ , are in the form that

$$y_{it} = d_{it}y_{it}^1 + (1 - d_{it})y_{it}^0, \quad (3.2)$$

where

$$d_{it} = \begin{cases} 1, & \text{if the } i\text{th unit is under treatment} \\ & \text{at time } t, \\ 0, & \text{otherwise.} \end{cases} \quad (3.3)$$

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as to whether a factor is strong or weak could be useful (e.g. Chudik, Pesaran and Tosetti (2010)), in practice, it is difficult to know if the extracted factors are strong or weak (or somewhere in between). Therefore, in this paper, we make the simplified assumption that the correlations among cross-sectional units are due to the presence of common factors,  $\underline{f}_t$  and the random idiosyncratic component for the  $i$ th unit,  $\epsilon_{it}$ , merely represents the impacts of  $i$ th unit-specific factors. In other words, we assume the factors that create the “local” dependence are also part of  $\underline{f}_t$ .

Let  $\underline{y}_t = (y_{1t}, \dots, y_{Nt})'$  be an  $N \times 1$  vector of  $y_{it}$  at time  $t$ . Suppose there is no intervention before  $T_1$ , then the observed  $\underline{y}_t$  takes the form that

$$\underline{y}_t = \underline{y}_t^0, \quad \text{for } t = 1, \dots, T_1. \quad (3.4)$$

Suppose at time  $T_1 + 1$ , there is a policy change for the  $i$ th unit. Without loss of generality, let this be the first unit that receives the treatment at time  $T_1 + 1$  and onwards,

$$y_{1t} = y_{1t}^1 \text{ for } t = T_1 + 1, \dots, T. \quad (3.5)$$

We assume other units are not affected by the policy intervention at the first unit, then

$$y_{it} = y_{it}^0 \text{ for } i = 2, \dots, N, \text{ for } t = 1, \dots, T. \quad (3.6)$$

We assume,

Assumption 5:  $E(\epsilon_{js} \mid d_{it}) = 0$ , for  $j \neq i$ .

A5 makes no claim about the relationship between  $d_{it}$  and  $\epsilon_{it}$ . They can be correlated. If so, the observed data are subject to selection on unobservables (e.g. Heckman and Vytlačil (2001)). They can be independent, then the observed data satisfy the conditional independence assumption of Rosenbaum and Rubin (1983). All we need for our approach is that the  $j$ th unit's idiosyncratic components are independent of  $d_{it}$  for  $j \neq i$ .

Under A1 - A5, we may predict  $y_{1t}^0$  by  $\hat{y}_{1t}^0 = \alpha_1 + b_1' \underline{f}_t$  for  $t = T_1 + 1, \dots, T$ , if we can identify  $\alpha_1, b_1$  and  $\underline{f}_t$ . If both  $N$  and  $T$  are large, we may use the procedure of Bai and Ng (2002) to identify the number of common factors,  $K$ , and estimate  $\underline{f}_t$  by the maximum likelihood procedure. Often, neither  $N$  nor  $T$  is large. In this situation, we suggest using  $\tilde{\underline{y}}_t = (y_{2t}, \dots, y_{Nt})'$  in lieu of  $\underline{f}_t$  to predict  $y_{1t}^0$ .

Let  $\underline{q}$  be a vector lying in the null space of  $B$ ,  $N(B)$ . We normalize the first element of  $\underline{q}$  to be 1 and denote  $\underline{q}' = (1, -\tilde{\underline{q}}')$ . If  $\underline{q} \in N(B)$ , then  $\underline{q}' B = 0$ , and

$$y_{1t}^0 = \bar{\alpha} + \tilde{\underline{q}}' \tilde{\underline{y}}_t + \epsilon_{1t} - \tilde{\underline{q}}' \tilde{\underline{\epsilon}}_t, \quad (3.7)$$

where  $\bar{\alpha} = \underline{a}'\alpha$ ,  $\tilde{y}_t = (y_{2t}, \dots, y_{Nt})'$ , and  $\tilde{\epsilon}_t = (\epsilon_{2t}, \dots, \epsilon_{Nt})'$ . Eq. (3.7) says that we can use  $\tilde{y}_t$  in lieu of  $\underline{f}_t$  to predict  $y_{1t}^0$ .

Then for any  $\underline{a} \in N(B)$ ,

$$y_{1t}^0 = E(y_{1t}^0 \mid \tilde{y}_t) + \epsilon_{1t}^*, \quad (3.8)$$

where

$$\begin{aligned} E(y_{1t}^0 \mid \tilde{y}_t) &= \bar{\alpha} + \tilde{a}'\tilde{y}_t + E(\epsilon_{1t} \mid \tilde{y}_t) - E(\tilde{a}'\tilde{\epsilon}_t \mid \tilde{y}_t) \\ &= \bar{\alpha} + \tilde{a}^{*'}\tilde{y}_t, \end{aligned} \quad (3.9)$$

$$\tilde{a}^{*'} = \tilde{a}'(I_{N-1} - \text{Cov}(\tilde{\epsilon}_t, \tilde{y}_t) \text{Var}(\tilde{y}_t)^{-1}) \quad (3.10)$$

$$\epsilon_{1t}^* = \underline{a}'\epsilon_t + \tilde{a}'[\text{Cov}(\tilde{\epsilon}_t, \tilde{y}_t) \text{Var}(\tilde{y}_t)^{-1}]\tilde{y}_t. \quad (3.11)$$

The  $\text{Var}(\cdot)$  and  $\text{Cov}(\cdot)$  denote the long-run variance and covariance. The variance of  $y_{1t}^0$  given  $\tilde{y}_t$  for  $\underline{a} \in N(B)$  is equal to

$$\text{Var}(y_{1t}^0 \mid \tilde{y}_t) = \text{Var}(\epsilon_{1t}) + \tilde{a}'[\text{Var}(\tilde{\epsilon}_t) - \text{Cov}(\tilde{\epsilon}_t, \tilde{y}_t) \text{Var}(\tilde{y}_t)^{-1} \text{Cov}(\tilde{y}_t, \tilde{\epsilon}_t)]\tilde{a}. \quad (3.12)$$

We note that  $(\bar{\alpha}, \tilde{a}^*)$  depends on  $\underline{a}$  for any  $\underline{a} \in N(B)$ . Since the minimum variance predictor depends on the choice of  $\underline{a}$  and covariance structure of  $\epsilon_t$ , we propose to choose  $\tilde{a}^*$  to minimize

$$\frac{1}{T_1}(y_1^0 - \underline{e}\bar{\alpha} - Y\tilde{a}^*)'A(y_1^0 - \underline{e}\bar{\alpha} - Y\tilde{a}^*), \quad (3.13)$$

where  $y_1^0 = (y_{11}, \dots, y_{1T_1})$ ,  $\underline{e}$  is a  $T_1 \times 1$  vector of 1's,  $Y$  is a  $T_1 \times (N-1)$  matrix of  $T_1$  time series observations of  $(\tilde{y}_t')$ , and  $A$  is a  $T_1 \times T_1$  positive definite matrix.

Assumption 6: For fixed  $K$  and  $N$ , there exists an  $\underline{a} \in N(B)$  such that in the neighborhood of  $\underline{a}$ ,

$$E\left[\frac{1}{T_1}(y_1^0 - \underline{e}\bar{\alpha} - Y\tilde{a}^*)'A(y_1^0 - \underline{e}\bar{\alpha} - Y\tilde{a}^*)\right], \quad (3.14)$$

has a unique minimum.

*Lemma 1:* Under A1 - A6, the solution of (3.13),  $(\hat{\alpha}, \hat{\tilde{a}}^*)$  converges to a  $(\bar{\alpha}, \tilde{a}^*)$  that corresponds to an  $\underline{a} \in N(B)$  as  $T_1 \rightarrow \infty$ .



**Proof:** From (3.8), we have  $y_{1t}^0 = \bar{\alpha} + \tilde{a}^{*'} \tilde{y}_t + \epsilon_{1t}^*$  and  $E(\epsilon_{1t}^* \mid \tilde{y}_t) = 0$ . Therefore, the minimum distance regression of  $y_{1t}$  on a constant and  $\tilde{y}_t$  yields consistent estimators for  $(\bar{\alpha}, \tilde{a}^{*'})$  when  $T_1 \rightarrow \infty$ . (e.g. Amemiya (1985)).

**Remark 3.1:** The null vectors in  $N(B)$  are not unique. However, for given  $A$  or objective function (3.13), the solution is unique. When  $A = I$ , our objective is to obtain the minimum variance predictor of  $y_{1t}^0$  given  $\tilde{y}_t$ . In other words, as pointed out by a referee, the conditional paths for the units under treatment are computed by exploiting only contemporaneous cross-sectional correlations. To allow the exploitation at leads and lags of the dynamic relationships among cross-sectional units, we may let  $A$  in (3.13) be a nondiagonal matrix, say the inverse of the covariance matrix of  $\xi_1^* = (\epsilon_{1i}^*, \dots, \epsilon_{1t}^*)'$ , and use the optimal forecasting formula of Goldberger (1962) to produce a counterfactual path that uses both current and lagged values of  $\tilde{y}_t$ . However, the so generated lead-lag relationships is restricted by the serial correlation patterns of  $\xi_1^*$  as compared to an unrestricted vector autoregressive model (VAR).

**Remark 3.2:** Although  $\bar{\alpha} = a' \alpha$  depends on the choice of  $a$ , it is just an unknown finite constant under A1 in the regression model (3.13). Therefore it can be treated as an unknown in (3.13).

When  $A = I$ , Lemma 1 suggests that we can predict  $y_{1t}^0$  by

$$\hat{y}_{1t}^0 = \hat{\alpha} + \hat{\tilde{a}}^{*'} \tilde{y}_t. \quad (3.15)$$

Therefore, we may predict  $\Delta_{1t}$  using

$$\hat{\Delta}_{1t} = y_{1t} - \hat{y}_{1t}^0 \text{ for } t = T_1 + 1, \dots, T. \quad (3.16)$$

*Lemma 2: Under A1-A6,*

$$E(\hat{\Delta}_{1t} \mid Y, \tilde{y}_t) = \Delta_{1t}, \quad t = T_1 + 1, \dots, T, \quad (3.17)$$

and

$$\text{Var} (\hat{\Delta}_{1t}) = \text{Var} (\epsilon_{1t}^*) + (1, \tilde{y}_t') \text{Cov} \begin{pmatrix} \hat{\alpha} \\ \hat{\tilde{a}}^* \end{pmatrix} \begin{pmatrix} 1 \\ \tilde{y}_t \end{pmatrix}. \quad (3.18)$$

**Proof:** Under A1-A6,

$$E \begin{pmatrix} \hat{\alpha} \\ \hat{\tilde{a}}^* \end{pmatrix} | Y = \begin{pmatrix} \bar{\alpha} \\ \tilde{a}^* \end{pmatrix}.$$

Lemma 2 follows from (3.9) and (3.12)

**Remark 3.3:** The counterfactuals  $y_{1t}^0, t = T_1 + 1, \dots, T$  depend on the individual specific effects  $\alpha_1$ , the common factors,  $\underline{f}_t$ , the individual specific response to time-varying common factors  $\underline{f}_t, \underline{b}_1$ , and the idiosyncratic component  $\epsilon_{1t}$ . However, the counterfactual predictor (3.15) does not require any of such knowledge, nor the dimension of  $\underline{f}_t$ . The information provided by  $\underline{f}_t$  is embedded in  $\tilde{y}_t$ . It follows that the predictor  $\hat{\Delta}_{1t}$ , (3.16), that uses  $\tilde{y}_t$  in lieu of  $\underline{f}_t$  allows the evaluation of policy interventions without the need to identify  $\underline{f}_t$  or  $B$ , which may be difficult in finite sample.

**Remark 3.4:** We do not make any assumption about  $\epsilon_{is}$  and  $d_{it}$ . All we need is that the policy intervention on the  $i$ th unit has no bearing on  $\epsilon_{jt}$  for  $j \neq i$  (Assumption 5). Hence, if the process (2.2) satisfies Assumptions 1-5, our proposed approach allows us to bypass the selection issue that has been a central concern in the program evaluation literature (e.g. Heckman and Hotz (1989), Heckman and Vytlačil (2001)).

**Remark 3.5:** When  $(T - T_1)$  is large, given A5, one can reverse the procedure to predict  $y_{1t}^1$  by  $E(y_{1t}^1 | \tilde{y}_t)$  for  $t = 1, \dots, T_1$ , where  $E(y_{1t}^1 | \tilde{y}_t)$  may be approximated by

$$\hat{y}_{1t}^1 = \hat{\alpha}^* + \hat{\tilde{a}}' \tilde{y}_t, \quad t = 1, \dots, T_1, \quad (3.19)$$

and construct the treatment effect had the policy intervention was in place before  $T_1$ ,  $\hat{\Delta}_{1t} = \hat{y}_{1t}^1 - y_{1t}, t = 1, \dots, T_1$ , where  $\hat{\alpha}^*$  and  $\hat{\tilde{a}}$  are estimated using data from  $T_1 + 1, \dots, T$ .

**Remark 3.6:** The synthetic control method for comparative case studies also use information of other individuals to construct the counterfactuals of treated individuals (e.g.

Abadie and Gardeazabal (2003), Card and Krueger (1994)). However, the focus and the approach are different. The synthetic approach assumes that (e.g. Abadie, Diamond and Hainmueller (2010))

$$y_{it}^0 = \delta_t + \underline{z}_i' \underline{\theta}_t + \underline{\mu}_i' \underline{\lambda}_t + \epsilon_{it}, \text{ for } i = 2, \dots, N, t = 1, \dots, T_1, T_1 + 1, \dots, T, \quad (3.20)$$

while for the first unit, they assume  $y_{1t}$  follows (3.20) for  $t = 1, \dots, T_1$ , and for  $t = T_1 + 1, \dots, T$ ,  $y_{1t}$  equals

$$y_{1t}^1 = \Delta_{1t} + \delta_t + \underline{z}_1' \underline{\theta}_t + \underline{\mu}_1' \underline{\lambda}_t + \epsilon_{1t} \text{ for } t = T_1 + 1, \dots, T, \quad (3.21)$$

where  $\delta_t$  is an unknown common factor with constant factor loading across units,  $\underline{z}_i$  is an  $(r \times 1)$  vector of observed covariates (not affected by the intervention),  $\underline{\theta}_t$  is an  $(r \times 1)$  vector of unknown parameters,  $\underline{\lambda}_t$  is a  $(K \times 1)$  vector of unobserved common factors,  $\underline{\mu}_i$  is a  $(K \times 1)$  vector of unknown factor loading and  $\Delta_{1t}$  is the treatment effect for the first unit. If we let  $\alpha_i = 0$ ,  $b_i' = (1, \underline{z}_i', \underline{\mu}_i')$  and  $f_t' = (\delta_t, \underline{\theta}_t', \underline{\lambda}_t')$  in (2.1), model (3.20) can be put in the form of (2.1). However, for (3.7) to hold, we need  $\underline{a}'B = 0$  that imposes the restriction  $\sum_{i=1}^N a_i = 0$ ,  $\sum_{i=1}^N a_i \underline{z}_i' = \underline{0}'$  and  $\sum_{i=1}^N a_i \underline{\mu}_i' = 0$ .

The synthetic control method constructs the predicted  $y_{1t}^0$  through  $\hat{y}_{1t}^0 = \sum_{i=2}^N a_i y_{it}$ , where the weights  $\tilde{\underline{a}}' = (a_2, \dots, a_N)$  are obtained by minimizing

$$(\underline{x}_1 - X\tilde{\underline{a}})'V(\underline{x}_1 - X\tilde{\underline{a}}) \quad (3.22)$$

subject to the constraints  $a_i \geq 0$  for  $i = 1, \dots, N$  and  $\sum_{j=2}^N a_i = 1$ , where  $\underline{x}_1$  is an  $(r + M) \times 1$  column vector consisting of the  $r$  observed covariates  $\underline{z}_1$  for the control (pre-treatment) period. To ensure unbiasedness of their estimator, under the assumption that the dimension of unknown common factors is  $K$ , they suggest including  $M$  other covariates in  $\underline{x}_1$  by constructing the time average of at least  $M$  such selectors through  $\bar{y}_1^m = \sum_{s=0}^{T_1} k_{1s}^m y_{1s}$ ,  $m = 1, \dots, M$ .  $X$  is an  $(r + M) \times (N - 1)$  matrix, a collection of all other  $\underline{x}_j$ ,  $j = 2, \dots, N$  columns similarly constructed as  $\underline{x}_1$  with  $\bar{y}_j^m = \sum_{s=0}^{T_1} k_{js}^m y_{js}$ ,  $m = 1, \dots, M$

(when  $k_{js}^m = \frac{1}{T_1}$ , then  $\bar{y}_j^m$  is just a simple pre-control time average). Therefore, the cross-sectional units weight  $a_i$  will be sensitive to the prior choice of  $z$ ,  $M$ , and  $k_{js}$ , hence the predicted  $\hat{y}_{1t}^0$ , or  $\hat{\Delta}_{1t}$ . Nor is the probability distribution of  $\hat{y}_{1t}^0$  or  $\hat{\Delta}_{1t}$  easily derivable. On the other hand, we suggest using regression method to choose  $\tilde{a}$  to mimic the behavior of treated individuals before the intervention as close as possible, say, by minimizing (3.13). As long as  $N$  is fixed, our procedure yields a unique weight  $\tilde{a}$  and unique  $\hat{y}_{1t}^0$ , hence unique  $\hat{\Delta}_{1t}$  with known probability distribution. Neither do we need to impose the constraint  $a_j \geq 0$ , nor  $\sum_{j=2}^N a_j = 1$ . Our approach can also easily be adapted to accommodate the case that some exogenous variables  $z_t$  also drive  $y_t$  by treating (2.2) conditional on  $z_t$ .

**Remark 3.7:** An alternative approach to exploit the correlation among the cross-sectional units is to construct a vector autoregressive model (VAR). A VAR can describe dynamic correlations generally. For instance, one can construct a VAR for  $y_t$ , as,

$$y_t^0 = \zeta + A_1 y_{t-1}^0 + \dots + A_p y_{t-p}^0 + u_t \quad (3.23)$$

Pre-intervention data can then be used to estimate the parameters of the system (3.23),  $\theta_{\text{pre-int}} = \text{vec}(\zeta, A_1, \dots, A_p)_{\text{pre-int}}$ ,  $\hat{\theta}_{\text{pre-int}}$ . The expected path of a cross-sectional unit in the absence of intervention, say  $y_{1t}^0$ , can then be constructed based on  $\hat{\theta}_{\text{pre-int}}$ . This approach has been adopted recently by Giannone, Lenza and Reichlin (2010) to evaluate the effect of policy intervention in the euro area. However, if there is a feedback relation from  $y_{1,t-j}^0$  to  $(y_{2t}^0, \dots, y_{Nt}^0)$  (i.e. the elements of the first column of  $A_j$  are nonzero (e.g. Granger (1969), Hsiao (1982))), substituting  $y_{1t}$  in lieu of  $y_{1t}^0$  in system (3.23) is likely to generate errors because the post-intervention  $y_{1,t-j}$  is actually  $y_{1,t-j}^1$ , not  $y_{1,t-j}^0$ . Moreover, if  $y_{1,t-j} = y_{1,t-j}^1$ , then  $(y_{2t}, \dots, y_{Nt})$  cannot be  $(y_{2t}^0, \dots, y_{Nt}^0)$ .

**Remark 3.8:** Model (2.2) with

$$f_t = H_1 f_{t-1} + \dots + H_q f_{t-q} + v_t \quad (3.24)$$

can be transformed into a VAR model (3.23). If the number of factors,  $K$ , is less than  $N$ , then it is possible to transform (3.23) into a one-way causal model from  $(y_{2t}^0, \dots, y_{Nt}^0)$  to  $y_{1t}^0$

(i.e. with all the elements of the first column of  $A_j$  equal to zero except for the first element for  $j = 1, \dots, p$ , Granger (1969)). However, if  $\underline{a}'B = \underline{0}'$ , so are  $\underline{a}'A_j = \underline{0}'$ ,  $j = 1, \dots, p$ , then  $y_{1t}^0$  will be just equal to (3.7).

**Remark 3.9:** If  $\underline{f}_t$  and  $\underline{b}_1$  are known, then  $\text{Var}(y_{1t}^0 | \underline{f}_t) = \text{Var}(\epsilon_{1t})$  is smaller than (3.12). If  $N$  and  $T$  are large, one can use Bai (2003), Bai and Ng (2002) procedure to identify the number of unknown factors  $K$  and estimate  $\underline{b}_1$  and  $\underline{f}_t$ . However, if  $T$  is small, then there could be sampling errors in identifying and estimating  $\underline{b}_1$  and  $\underline{f}_t$ . It may be better to use  $\tilde{\underline{y}}_t$  and  $\tilde{\underline{a}}$  in lieu of  $\underline{b}_1$  and  $\underline{f}_t$  as demonstrated in our Monte Carlo studies in section 5 (also see Pesaran, Smith and Smith (2007)).

#### 4. Tests for Significance of Policy Intervention

The predictor for the effectiveness of social policy (3.16) allows the effects of such a policy to vary over time. From the estimated  $\Delta_{1t}$ , we may use time series techniques to evaluate the evolution of policy effects over time.

Assumption 7:  $\{\epsilon_{it}\}$  is weakly dependent (mixing) for all  $i$ .

Suppose the treatment effects,  $\Delta_{1t}$ , follow an autoregressive - moving average model (ARMA) of the form,

$$a(L)\Delta_{1t} = \mu + \theta(L)\eta_t, \quad (4.1)$$

where  $L$  is the lag operator,  $\eta_t$  is an i.i.d. process with zero mean and constant variance and the roots of  $\theta(L) = 0$  lie outside the unit circle. If the roots of  $a(L) = 0$  all lie outside the unit circle, the treatment effect is stationary, and the long-term treatment effect is

$$\Delta_1 = a(L)^{-1}\mu = \mu^*. \quad (4.2)$$

If one of the roots of  $a(L) = 0$  lies on the unit circle, the intervention effects are integrated of order 1,  $I(1)$ .

From the estimated  $\hat{\Delta}_{1t}$ , we can use the Box-Jenkins (1970) procedure to construct a time series model,

$$\tilde{a}(L)\hat{\Delta}_{1t} = \tilde{\mu} + \tilde{\theta}(L)v_t, \quad (4.3)$$

where  $v_t$  is i.i.d. with mean zero and variance  $\sigma_v^2$ .

*Lemma 3:* Suppose the roots of  $a(L) = 0$  lie outside the unit circle, under A1 - A6, when both  $T_1$  and  $(T - T_1)$  go to infinity,

$$\text{plim } \tilde{a}(L)^{-1} \tilde{\mu} = \text{plim } \hat{\mu}^* = \mu^* = a(L)^{-1} \mu \quad (4.4)$$

and

$$\sqrt{T - T_1}(\hat{\mu}^* - \mu^*) \sim N(0, \sigma_{\mu^*}^2), \quad (4.5)$$

where

$$\sigma_{\mu^*}^2 = \frac{\partial \mu^*}{\partial \gamma'} \text{Var} \left( \sqrt{T - T_1} \hat{\gamma} \right) \frac{\partial \mu^*}{\partial \gamma}, \quad (4.6)$$

and  $\gamma = (\tilde{\mu}, \tilde{a}_1, \dots, \tilde{a}_p)$ , assuming  $\tilde{a}(L)$  is of  $p$ -th order.

**Proof:** If  $\underline{y}_t$  is stationary, the estimators of  $(\hat{\alpha}, \hat{\alpha}^*)'$  are  $\sqrt{T_1}$ -consistent. If  $\underline{y}_t \sim I(1)$  and not cointegrated, the estimator of  $\hat{\alpha}$  remain  $\sqrt{T_1}$ -consistent, but  $\hat{\alpha}^*$  is  $T_1$ -consistent (e.g. Phillips and Durlauf (1986)). Either way,

$$y_{1t}^0 - \hat{y}_{1t}^0 = \epsilon_{1t}^* + O(T^{-\frac{1}{2}}). \quad (4.7)$$

Adding and subtracting yields

$$\hat{\Delta}_{1t} = y_{1t} - \hat{y}_{1t}^0 = \Delta_{1t} + \epsilon_{1t}^* + o(1). \quad (4.8)$$

Substituting (4.8) into (4.1) yields

$$a(L)\hat{\Delta}_{1t} = \mu + \theta(L)\eta_t + a(L)\epsilon_{1t}^* + o(1). \quad (4.9)$$

Since  $\epsilon_{1t}^*$  is a mean zero  $I(0)$  process, we obtain (4.2) by approximating  $\theta(L)\eta_t + a(L)\epsilon_{1t}^*$  by a  $q$ -th order moving average process,  $\theta^*(L)v_t$ . If the roots of  $\theta^*(L)$  all lie outside the unit circle,  $\hat{\Delta}_{1t}$  can also be approximated by an AR process,

$$\tilde{a}(L)\hat{\Delta}_{1t} = \tilde{\mu} + v_t, \quad (4.10)$$

where  $\tilde{a}(L) = \theta^*(L)^{-1}a(L)$  and  $\tilde{\mu} = \theta^*(L)^{-1}\mu$ .

Under fairly general conditions, the maximum likelihood estimator (MLE) of  $a(L)$ ,  $\theta^*(L)$  and  $\mu$  are consistent and asymptotically normally distributed. The asymptotic variance,  $\sigma_{\mu^*}^2$ , can then be derived by using the delta method (e.g. Rao (1973, ch. 2)).

If the treatment effects is a stationary process (i.e. the roots of  $a(L) = 0$  all lie outside the unit circle), the long-term impact of the intervention can also be estimated by taking the simple average of the treatment effects.

*Lemma 4:* Suppose all the roots of  $a(L) = 0$  lie outside the unit circle, under A1 - A6, when both  $T_1$  and  $(T - T_1)$  go to infinity,

$$\begin{aligned} \text{plim} \quad & \frac{1}{T-T_1} \sum_{t=T_1+1}^T \hat{\Delta}_{1t} = \Delta_1 \\ (T - T_1) \rightarrow \infty \end{aligned} \tag{4.11}$$

The variance of (4.11) can be approximated by the heteroscedastic-autocorrelation consistent (HAC) estimator of Newey and West (1987).

**Proof:** Given (3.17) and (3.18), the law of large number holds.

## 5. Choice of Cross-Sectional Units

### 5.1 Modeling Strategy

Often there are large number of cross-sectional units that can be used to predict  $y_{1t}^0$  (or that are generated according to (2.1) or (2.2)). Intuitively, it would appear to favor using as many available cross-sectional units as possible as long as  $T > N$ . This will be the case when the number of common factors,  $K$ , is fixed,  $T_1$  goes to infinity, and  $\frac{N}{T_1} \rightarrow 0$ . However, if  $T_1$  or  $\frac{N}{T_1}$  is finite, there may be an advantage to use only a subset of available cross-sectional units to predict the counterfactuals, in particular, if the data generating processes for cross-sectional units satisfy the condition of Lemma 5 (ii) below.

Let there be  $m$  cross-sectional units that optimally predict  $y_{1t}^0$  and  $(N - m - 1)$  remaining cross-sectional units that could also be included to predict  $y_{1t}^0$ . Let  $Y_1$  and  $Y_2$

be the  $T_1 \times m$  and  $T_1 \times (N - m - 1)$  time series observations for these  $m$  cross-sectional unit and  $(N - m - 1)$  cross-sectional units, respectively, then

$$Y_1 = FB'_1 + \mathcal{E}_1, \quad (5.1)$$

and

$$Y_2 = FB'_2 + \mathcal{E}_2, \quad (5.2)$$

where the  $t$ th-row of  $F$  takes the form  $(1, f'_t)$  and the  $i$ th column of  $B'_1$  and  $B'_2$  take the form  $(\alpha_i, b'_i)'$ , and  $\mathcal{E}_1$  and  $\mathcal{E}_2$  denote the  $T_1 \times m$  and  $T_1 \times (N - m - 1)$  idiosyncratic components of  $Y_1$  and  $Y_2$ , respectively.

*Lemma 5:* Under A1 - A5,

- (i) The optimal number of cross-sectional units for constructing  $y_{1t}^0$  is  $K \leq m \leq N - 1$
- (ii) If  $B_2(B'_1\Theta_1^{-1}B'_1 + I_K)^{-1} \begin{pmatrix} \alpha_1 \\ b_1 \end{pmatrix} = 0$  then  $Y_2$  yields no predictive power for  $E(y_1 | Y_1)$ , where  $\Theta_1 = E(\mathcal{E}'_1\mathcal{E}_1)$ .

For proof, see Appendix A.

When  $N$  is fixed and  $T_1 \rightarrow \infty$ , the least squares estimator of  $(y_1 - Y_1a_1 - Y_2a_2)'(y_1 - Y_1a_1 - Y_2a_2)$  yields  $\hat{a}_2$  that will converge to 0 under the condition of Lemma 5 (ii). In other words, one can use all  $(N - 1)$  available cross-sectional units to predict  $y_{1t}^0$ . However, in many occasions,  $T_1$  is finite. As more cross-sectional units are used, the variance of  $\tilde{a}^*$  will also increase. To balance the within-sample fit with post-sample prediction error, we suggest the following model selection strategy (Hsiao and Wan (2009)):

Step 1: Use  $R^2$  or likelihood values to select the best predictor for  $y_{1t}^0$  using  $j$  cross-sectional units out of  $(N - 1)$  cross-sectional units, denoted by  $M(j)^*$ , for  $j = 1, \dots, N - 1$ .<sup>4</sup>

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<sup>4</sup>Given  $N$ , there are  $2^N$  possible combinations. Step 1 is proposed to reduce the number of predictive models. An alternative is to use some “boosting method (Buhlmann (2006))” or “LASSO (Tibshirani (1996))” or to use some targeted predictors based on some soft and hard-thresholding as suggested by a referee.



Step 2: From  $M(1)^*, M(2)^*, \dots, M(N-1)^*$ , choose  $M(m)^*$  in terms of some model selection criterion.

## 5.2 Monte Carlo Studies

Under the assumption that  $\underline{y}_t$  is generated by a factor model of the form (2.2), in this sub-section we compare the predictive performance of our approach versus the approach of first determining the number of factors,  $K$ , and identifying  $\alpha_1$  and  $\underline{b}_1$ , then use the estimated  $\underline{f}_t, \alpha_1$ , and  $\underline{b}_1$  to generate the counterfactuals when  $N$  and  $T$  are small.

First, we wish to see if there is a need to use all cross-sectional units using our approach. There are a number of model selection criteria one can use to select the best approximating model. In this section we conduct a small scale Monte Carlo to examine the performance of Akaike information criterion (AIC) (Akaike (1973, 1974)), and AICC (Hurvich and Tsai (1989)), by comparing the post-intervention mean square prediction error

$$PMSE(p) = \frac{1}{T - T_1} \sum_{t=T_1+1}^T (y_{1t}^0 - \hat{y}_{1t}^0(p))^2, \quad (5.3)$$

where  $\hat{y}_{1t}^0(p)$  is generated by using  $p$  cross-sectional units data of  $y_{it}$  for  $t = 1, \dots, T_1$  to obtain the least square estimates of  $\tilde{a}_p^*$ , then  $\hat{y}_{1t}^0(p) = \hat{\tilde{a}}_p^{*'} Y_t$ ,  $t = T_1 + 1, \dots, T$ .

To see which model selection criterion works better, we generate model (2.1) with  $N = 21$  countries, the sum of the dimension of both  $Y_1$  and  $Y_2$ . We use  $T_1 = 25, 40$ , and  $60$  observations, the number of pre-intervention periods to approximate the path of  $y_1$  before intervention. The OLS estimators are then used to predict  $y_{1t}^0$  for the post-intervention period which has  $T - T_1 = 10$  periods. Four different factor structures are used. The first one consists of two ( $K = 2$ ) stationary factors:

$$\begin{aligned} f_{1t} &= 0.3f_{1,t-1} + u_{1t} \\ f_{2t} &= 0.6f_{2,t-1} + u_{2t} \end{aligned} \quad (5.4)$$

where the innovation for factor loadings  $u_t$  and the idiosyncratic errors  $\epsilon_t$  are generated

by  $N(0, 1)$  and  $\sigma N(0, 1)$ , respectively. The second one is another set of stationary factors:

$$\begin{aligned} f_{1t} &= 0.8f_{1,t-1} + u_{1t} \\ f_{2t} &= -0.6f_{2,t-1} + u_{2t} + 0.8u_{2t-1} \\ f_{3t} &= u_{3t} + 0.9u_{3t-1} + 0.4u_{3t-2}. \end{aligned} \tag{5.5}$$

The third has an i.i.d. factor. The last one has an almost non-stationary factor:

$$f_{1t} = 0.95f_{1,t-1} + u_{1t}. \tag{5.6}$$

In all the above cases,  $b_i \sim N(1, 1)$ .

Two model selection criteria are compared:

$$AIC(p) = T_1 \ln \left( \frac{\epsilon'_0 \epsilon_0}{T_1} \right) + 2(p + 2) \tag{5.7}$$

$$AICC(p) = AIC(p) + \frac{2(p + 2)(p + 3)}{T_1 - (p + 1) - 2} \tag{5.8}$$

where  $p$  is the number of countries included;  $\epsilon_0$  denote the OLS residuals.

We repeat the experiment for each of the four data generating process five-hundred times. All four simulation results show that the pre-intervention MSE decreases when  $p$  increases, whereas post-intervention MSE decreases initially and then increases when  $p$  increases. Denote the optimal number of countries chosen as  $m$ . The results are summarized in Tables 1-4. For all the experiments, the average  $m$  is between  $K$  and  $N - 1$ . This is consistent with the notion of the bias and variance tradeoff. The frequency distributions show that not once all 20 cross-sectional units are selected in terms of AICC and around 1% chance the 20 units models are chosen in terms of AIC. On average, between 4 and 6 cross-sectional units are chosen in terms of AICC and 6 to 12 cross-sectional units are chosen in terms of AIC. When  $T_1$  is small, say 25 or 40, the PMSE in terms of models chosen by AICC and AIC are significantly smaller than the models using all 20 cross-sectional units. When  $T_1$  becomes large, say 60, models using all 20 cross-sectional units have PMSE converge towards the PMSE of the optimally chosen models in terms of AICC or AIC, but

the PMSE based on 20 cross-sectional units are still larger than those based only on  $m$  cross-sectional units. These Monte Carlo studies appear to support the theoretical finding that optimal  $m$  is between  $K$  and  $(N - 1)$  when  $T_1$  is finite. When  $\frac{N}{T_1} \rightarrow 0$ , then using all available cross-sectional units will be fine because the estimated  $\hat{a}_2$  will converge to zero.

We then compare the predictive performance of our approach based on AIC, and AICC with Bai and Ng (2002) PC and IC criteria. Tables 5 and Table 6 provide the results of one factor model based on setting maximum number of  $K$  equal to 8 and 20, respectively. As one can see the predictive performance of Bai and Ng (2002) is very sensitive to the prior specified number of maximum  $K$ . The performance of factor model also deteriorates when the number of factors increased from 1 to 5 (Tables 6 and 7); when the average of  $b_i$  changed from 0 to 0.3 or 1 (Tables 9 and 10); when the distribution of  $b_i$  changed to Uniform  $(-1, 1)$  or  $N(2, 2)$  (Table 8 and 11); when the idiosyncratic components,  $\epsilon_{it}$ , have heteroscedastic variances or serially correlated (Table 12 and 13) and signal-to-noise ratio reduces (Table 15). However, the performance of factor model does improve when  $T$  increases (Table 14).

In short, when  $N$  and  $T$  are finite, the limited Monte Carlos show that generating counterfactuals based on a factor model using Bai and Ng (2002) model selection strategy appears to be sensitive to (a) the signal-to-noise ratio; (b) the distribution of factor loading matrix,  $B$ ; (c) the average values of  $B, \frac{1}{N} \sum_{i=1}^N b'_i$ ; (d) the number of unknown factors,  $K$ ; (e) the *a priori* assumed maximum number of unknown factors; (f) the serial correlations of the idiosyncratic components,  $\epsilon_{it}$ ; and (g) the heteroscedasticity of  $\epsilon_{it}$ . On the other hand, our procedure of using  $\tilde{y}_{it}$  in lieu of  $f_t$  does not appear to be affected by any of these issues. On average, they yield much smaller prediction errors than the factor approach.

## 6. Data

Because Hong Kong, by comparison, is a tiny city relative to other countries and regions, we believe whatever happened in Hong Kong will have no bearing to other countries. In other words, we expect Assumption 5 to hold. Therefore, we use quarterly real

growth rate of Australia, Austria, Canada, China, Denmark, Finland, France, Germany, Indonesia, Italy, Japan, Korea, Malaysia, Mexico, Netherlands, New Zealand, Norway, Philippines, Singapore, Switzerland, Taiwan, Thailand, UK, and US to predict the quarterly real growth rate of Hong Kong in the absence of intervention. All the nominal GDP, CPI are from OECD Statistics, International Financial Statistics and CEIC Data base.

There are many ways to compute quarterly growth rates. One can either measure the change compared with the corresponding quarter in the previous year (year-on-year) or measure the change since the previous quarter (e.g. Neo (2003)). We note that the four quarters within one year have different numbers of working days and different countries have different seasonal effects on production and expenditure. For instance, Chinese new year always falls in the first quarter and it is a big holiday for Hong Kong, virtually all business and government agencies are closed for celebration, but not so for other countries. Since our data are non-seasonally adjusted and our interest is in finding the long term trend, we compute the quarterly growth rate by measuring the change compared with the corresponding quarter in the previous year.

## 7. Empirical Analysis

In this section we illustrate the use of our panel data approach for program evaluation by considering the impact on Hong Kong real GDP growth rate with the revert of sovereignty on July 1, 1997 from U.K. to China and the implementation of CEPA starting in 2004-Q1 between the Mainland China and Hong Kong. (We present the evaluation using the factor approach in Appendix B.) We first wish to evaluate the impact of change of sovereignty on real GDP had Hong Kong stayed under British rule. Since there are only 18 observations between 1993Q1 and 1997Q2, we limit the countries under consideration for constructing counterfactuals to China, Indonesia, Japan, Korea, Malaysia, Philippines, Singapore, Taiwan, Thailand and US — countries that are either in the region or economically closely associated with Hong Kong. Using AICC, we select Japan, Korea, US and Taiwan to construct the hypothetical growth path of Hong Kong had there been no change

of sovereignty. The OLS weights based on 1993Q1 - 1997Q2 data are reported in Table 16 and the estimated treatment effects are reported in Table 17. The actual and hypothetical growth paths for the period 1993Q1 - 1997Q2, and 1997Q3 - 2003Q4 are plotted in Figure 1 and 2, respectively. Because the treatment effects appears to be serially correlated (see figure 3), we fit an AR(2) model for the estimated treatment effects:

$$\hat{\Delta}_{1t} = \begin{matrix} -.0063 + \\ (.0068) \end{matrix} \begin{matrix} 1.459 \hat{\Delta}_{1,t-1} - \\ (0.1559) \end{matrix} \begin{matrix} .6547 \hat{\Delta}_{1,t-2} + \hat{\eta}_t \\ (.1558) \end{matrix} \quad (6.1)$$

where estimated standard errors are in parentheses. The implied long-run effects is -.032. However, the  $t$ -statistic is only -1.04, not statistically significant.

Using the AIC criterion, the selected countries are Japan, Korea, Philippines, Taiwan and the US. The OLS estimates of the weights are in Table 18 and treatment effects are in Table 19, respectively. The actual and hypothetical growth paths for 1993Q1 - 1997Q2 and 1997Q3 - 2003Q4 are plotted in Figures 4 and 5, respectively. Again, the estimated treatment effects appear serially correlated. The fitted AR(2) model takes the form

$$\hat{\Delta}_{1t} = \begin{matrix} -.0066 + \\ (.0078) \end{matrix} \begin{matrix} 1.3821 \hat{\Delta}_{1,t-1} - \\ (.1722) \end{matrix} \begin{matrix} 0.5764 \hat{\Delta}_{1,t-2} + \hat{\eta}_t \\ (.1722) \end{matrix} \quad (6.2)$$

The implied long-run effect is -0.033. However, the  $t$ -statistic is only -.94, which is not statistically significant.

The real GDP growth in Hong Kong appears to be approximated well by the chosen controls before treatment by either criterion. The estimated treatment effects are not statistically significant. Therefore, we may conclude that the political integration of Hong Kong with Mainland China do not appear to have any significant impact on Hong Kong's economic growth. The lack of intervention effects is hardly surprising given the "one country, two systems" concept proposed by Deng Xiaoping. It is generally recognized that apart from change of national flags, Hong Kong's institutional arrangements were basically left untouched during this period. Moreover, the change of sovereignty was known fourteen years in advance and the institutional arrangements were laid down in great detail in the

Sino-British Joint Declaration of 1984. Presumably, all needed adjustments had already taken place before 1997.

Given we do not find any effect of the change of sovereignty, we can pool the data of 1993Q1 to 2003Q4 to examine the effect of the CEPA including Individual Travel Scheme and Removal of Preferential Tariff which was signed on June 29, 2003, but implementation only started on January 1, 2004. Since we now have more degrees of freedom, we can use the model selection strategy discussed in section 5 to generate the hypothetic growth path for Hong Kong had there been no CEPA with Mainland China. Using the AICC criterion, the countries selected are Austria, Italy, Korea, Mexico, Norway and Singapore. OLS estimates of the weights are reported in Table 20. Actual and predicted growth path from 1993Q1 to 2003Q4 are plotted in Figure 7. The availability of more pre-intervention period data appears to allow more accurate estimates of the country weights and better tracing of the pre-intervention path. The estimated quarterly treatment effects are reported in Table 21. The actual and predicted counterfactuals for the period 2004Q1 to 2008Q1 are presented in Figure 8. Using the AIC criterion, the selected group consists of Austria, Germany, Italy, Korea, Mexico, Norway, Philippines, Singapore and Switzerland. The OLS estimates of the weights are in Table 22 and the estimated quarterly treatment effects are in Table 23. The pre- and post intervention actual and predicted outcomes are plotted in Figures 10 and 11. It is notable that both groups of countries trace closely the actual Hong Kong path before the implementation of CEPA (with  $R^2$  above .93). It is also quite remarkable that the post-sample predictions closely matched the actual turning points at a lower level for the treatment period even though no Hong Kong data were used. The CEPA effect at each quarter was all positive and appeared to be serially uncorrelated, see Figures 9 and 12. The average actual growth rate from 2004Q1 - 2008Q1 is 7.26%. The average projected growth rate without CEPA is 3.23% using the group of countries selected by AICC and 3.47% using the group selected by AIC. The estimated average treatment effect is 4.03% with a standard error of 0.016 based on the AICC group and 3.79% with a

standard error of 0.0151 based on the AIC group. The  $t$ -statistic is 2.5134 for the former group and 2.5122 for the latter group. Either set of countries yields similar predictions and highly significant CEPA effects. In other words, through liberalization and increased openness with Mainland China, the real GDP growth rate of Hong Kong is raised by more than 4% compared to the growth rate had there been no CEPA agreement with Mainland China.

The Hong Kong government statistics appear to corroborate this finding. A recent Hong Kong Legislative Council paper (LC Paper No. CD(1) 1849/06-07(04)) shows that the tariff-free access of goods produced in Hong Kong has stimulated rising capital investment from HK\$103 million in 2005, to HK\$202 million in 2006 and HK\$239 million in 2007. Liberalization to trade in services has further stimulated capital investment. Capital investments in transport, logistics, distribution, advertising and construction stood at HK\$1.0 billion in 2004, but were at HK\$2.4 billion in 2007. The Individual Visit Scheme (IVS) has led to a substantial increase of tourism from China. From the implementation of the scheme to the end of 2006, Mainland Chinese visitors have made 17.2 million trips to Hong Kong. IVS visitors spending in 2006 was HK\$9.3 billion, about 38% higher than 2004. Moreover, the implementation of CEPA also helped to rebuild confidence in the economy after a prolonged period of economic stagnation. For instance, the value of total receipts for the restaurant sector in 2008Q1 was up by 15.8% compared with 2007Q1 and the value of total retail sales in March, 2008 increased by 20% compared with a year earlier. If the fundamental relations between the aggregate and components stay the same before and after 2004Q1, then one should expect the relative contribution of additional unit increase of each component to the aggregates should stay the same in those two periods and the impact of CEPA would be on its impact on the value of each component. However, a simple sectoral analysis of regressing  $\log(\text{real GDP})$  on  $\log(\text{Re-Export from China})$ ,  $\log(\text{Import})$  and  $\log(\text{Number of visitors})$  also show a statistically significant change of the impact of  $\log(\text{Number of Chinese Visitors})$  from 0.0638 in pre-CEPA period to 0.1663 for

the post-CEPA period with highly significant  $t$ -values. In other words, it appears that IVS is the most important component of CEPA and its impact not just on increasing tourist revenue, but serves to raise the confidence level of Hong Kong consumers and investors. As a result, the unemployment rate has dropped from 7.9% in 2003 to 4.8% in 2006 and 4.2% in September-November 2007. The per-capita income in 2006 reached US\$27,604. The Hang Seng Index at the end of 2007 reached 27812.

## 8. Conclusion

In this paper we have proposed a panel data approach to assess the impact of a policy intervention. We demonstrate that the dependence among cross-sectional units can be utilized to construct the counterfactuals. We identify the source of cross-sectional correlations through a factor framework. However, if sample size is finite, there may be an advantage to just use observed  $\underline{y}_t$  because the impacts of unobserved factors,  $\underline{f}_t$ , are already embedded in  $\underline{y}_t$ . In this approach, there is no need to distill the fundamental factors and their factor loading matrix as in Bai (2003), Bai and Ng (2002), Bernanke and Boivin (2003)), etc. The method is easy to implement and inference appears quite robust.

We illustrate our methodology by considering the political and economic intervention effects on Hong Kong's economy. We find that the change of sovereignty in 1997 hardly had any impact on Hong Kong's economy. On the other hand, the implementation of CEPA agreement in 2004 has a significant impact. Hong Kong's real GDP growth rate is 4% higher than what would have happened in the absence of CEPA.



## APPENDIX A

In this Appendix, we prove Lemma 6. Using the notation of section 5, decompose  $Y = (Y_1, Y_2)$ . Noting that  $\underline{a} = (BB' + \Theta)^{-1}B\tilde{\underline{b}}_1'$  and  $\underline{a}_1 = (B_1B_1' + \Theta_1)^{-1}B_1\tilde{\underline{b}}_1'$  minimize  $E[\underline{y}_1^0 - Y\underline{a}]'[\underline{y}_1^0 - Y\underline{a}]$  and  $E[\underline{y}_1^0 - Y_1\underline{a}_1]'[\underline{y}_1^0 - Y_1\underline{a}_1]$ , respectively, where  $\tilde{\underline{b}}_1' = (1, \underline{b}_1')$ , and  $\Theta = E(\underline{\epsilon}\underline{\epsilon}') = \begin{bmatrix} \Theta_1 & 0 \\ 0 & \Theta_2 \end{bmatrix}$ . Then

$$\text{MSE}(Y_1) = \sigma_1^2 + \tilde{\underline{b}}_1'[I - B_1'(B_1B_1' + \Theta_1)^{-1}B_1]\tilde{\underline{b}}_1, \quad (\text{A.1})$$

$$\text{MSE}(Y) = \sigma_1^2 + \tilde{\underline{b}}_1'[I - B'(BB' + \Theta)^{-1}B]\tilde{\underline{b}}_1. \quad (\text{A.2})$$

We first show that if  $m < K$ , then  $\text{MSE}(Y) < \text{MSE}(Y_1)$ ,  $\text{MSE}(Y) < \text{MSE}(Y_1)$  holds *iff*

$$\begin{aligned} I - B'(BB' + \Theta)^{-1}B &< I - B_1'(B_1B_1' + \Theta_1)^{-1}B_1 \\ \iff \begin{pmatrix} (B_1B_1' + \Theta_1)^{-1} & 0 \\ 0 & 0 \end{pmatrix} - \begin{pmatrix} B_1B_1' + \Theta_1 & B_1B_2' \\ B_2B_1' & B_2B_2' + \Theta_2 \end{pmatrix}^{-1} &< 0 \\ \iff \begin{pmatrix} A & X \\ X' & C \end{pmatrix} &< 0, \end{aligned} \quad (\text{A.3})$$

where

$$A = (B_1B_1' + \Theta_1)^{-1} - (B_1M_2B_1' + \Theta_1)^{-1}$$

$$X = (B_1M_2B_1' + \Theta_1)^{-1}B_1B_2'(B_2B_2' + \Theta_2)^{-1}$$

$$X' = (B_2B_2' + \Theta_2)^{-1}B_2B_1'(B_1M_2B_1' + \Theta_1)^{-1}$$

$$C = -(B_2B_2' + \Theta_2)^{-1}B_2B_1'(B_1M_2B_1' + \Theta_1)^{-1}B_1B_2'(B_2B_2' + \Theta_2)^{-1} - (B_2B_2' + \Theta_2)^{-1}$$

$$M_2 = I_K - B_2'(B_2B_2' + \Theta_2)^{-1}B_2$$

$$M_2 = I_K - B_2'(B_2B_2' + \Theta_2)^{-1}B_2 = I_K - B_2'D^{-\frac{1}{2}}D^{-\frac{1}{2}}B_2 \equiv I_K - U'U, \text{ where}$$

$$U = D^{-\frac{1}{2}}B_2 \text{ and } D = B_2B_2' + \Theta_2.$$

By Theorem A.3.5 (See P.639 of Anderson (2003)), the conditions for  $I_K - U'U$  and  $I_L - UU'$  to be positive definite are the same. Thus,

$$I_L - UU' = I_L - D^{-\frac{1}{2}} B_2 B_2' D^{-\frac{1}{2}} > 0 \iff D - B_2 B_2' = \Theta_2 > 0.$$

Since the last statement holds, we conclude that  $M_2 > 0$ .

$$P_2 \equiv I_K - M_2 = B_2'(B_2 B_2' + \Theta_2)^{-1} B_2 > 0$$

Thus,  $(B_1 B_1' + \Theta_1) - (B_1 M_2 B_1' + \Theta_1) = B_1(I_K - M_2)B_1' = B_1 P_2 B_1' > 0$ . Then,  $A = (B_1 B_1' + \Theta_1)^{-1} - (B_1 M_2 B_1' + \Theta_1)^{-1} < 0$

$$-C = (B_2 B_2' + \Theta_2)^{-1} B_2 B_1' (B_1 M_2 B_1' + \Theta_1)^{-1} B_1 B_2' (B_2 B_2' + \Theta_2)^{-1} + (B_2 B_2' + \Theta_2)^{-1} > 0.$$

$$\iff B_2 B_1' (B_1 M_2 B_1' + \Theta_1)^{-1} B_1 B_2' (B_2 B_2' + \Theta_2)^{-1} + I_L > 0$$

$$\iff B_2 B_1' (B_1 M_2 B_1' + \Theta_1)^{-1} B_1 B_2' + (B_2 B_2' + \Theta_2) > 0$$

$$\iff B_2 [B_1' (B_1 M_2 B_1' + \Theta_1)^{-1} B_1 + I_K] B_2' + \Theta_2 > 0$$

Therefore,  $C$  is a negative definite matrix.

$$\text{The Schur Complement } S = -C - (-X')(-A)^{-1}(-X) = -(C - X'A^{-1}X)$$

$$S = (B_2 B_2' + \Theta_2)^{-1} B_2 B_1' G^{-1} B_1 B_2' (B_2 B_2' + \Theta_2)^{-1} + (B_2 B_2' + \Theta_2)^{-1} \\ + (B_2 B_2' + \Theta_2)^{-1} B_2 B_1' G^{-1} [H^{-1} - G^{-1}]^{-1} G^{-1} B_1 B_2' (B_2 B_2' + \Theta_2)^{-1}$$

$$(B_2 B_2' + \Theta_2) S (B_2 B_2' + \Theta_2) \\ = B_2 B_1' G^{-1} B_1 B_2' + (B_2 B_2' + \Theta_2) + B_2 B_1' G^{-1}]^{-1} G^{-1} (H^{-1} - G^{-1}) G^{-1} B_1 B_2' \\ = B_2 B_1' G^{-1} B_1 B_2' + (B_2 B_2' + \Theta_2) + B_2 B_1' [G(H^{-1} - G^{-1})G]^{-1} B_1 B_2' \\ = B_2 B_1' G^{-1} B_1 B_2' + (B_2 B_2' + \Theta_2) + B_2 B_1' [GH^{-1}G - G]^{-1} B_1 B_2' \\ = B_2 B_1' [G^{-1} - (GH^{-1}G - G)^{-1}] B_1 B_2' + (B_2 B_2' + \Theta_2)$$

where  $G = B_1 M_2 B_1' + \Theta_1$  and  $H = B_1 B_1' + \Theta_1$ . To see if  $RHS > 0$ , we need to check  $G^{-1} - (GH^{-1}G - G)^{-1} > 0$ .

Note that  $GH^{-1}G - G = G(H^{-1}G - I_K) < 0$  because:

$$H^{-1}G = (B_1 I_K B_1' + \Theta_1)^{-1}(B_1 M_2 B_1' + \Theta_1) < I_K \text{ since } I_K - M_2 > 0.$$

Then,  $G^{-1} - (GH^{-1}G - G)^{-1} > 0$

$$\iff G^{-1} > (GH^{-1}G - G)^{-1} = (H^{-1}G - I_K)^{-1}G^{-1}$$

$$\iff I_K > (H^{-1}G - I_K)^{-1}$$

which is always true. Therefore,  $S > 0$ . By the positivity of Schur Complement, (A.3) holds. Therefore,  $m > K$ .

We now show that given the optimal choice of  $m$  cross-sectional units, any additional cross-sectional units yield no predictive power.

Rewrite

$$MSE(Y) = E(\underline{y}_1^0 - Y_1 \underline{a}_1 - Y_2 \underline{a}_2)'(\underline{y}_1^0 - Y_1 \underline{a}_1 - Y_2 \underline{a}_2) \quad (\text{A.4})$$

Minimizing (A.4) yields

$$\underline{a}_1 = (B_1 B_1' + \Theta_1)^{-1}(B_1 \tilde{\underline{b}}_1 - B_1 B_2' \underline{a}_2), \quad (\text{A.5})$$

and

$$\underline{a}_2 = (B_2 B_2' + \Theta_2)^{-1}(B_2 \tilde{\underline{b}}_1 - B_2 B_1' \underline{a}_1). \quad (\text{A.6})$$

Substituting (A.5) into (A.6) yields

$$\begin{aligned} & [(B_2 B_2' + \Theta_2) - B_2 B_1' (B_1 B_1' + \Theta_1)^{-1} B_1] \underline{a}_2 \\ &= B_2 (I - B_1' (B_1 B_1' + \Theta_1)^{-1} B_1) \tilde{\underline{b}}_1 \\ &= B_2 (B_1' \Theta_1^{-1} B_1 + I_K)^{-1} \tilde{\underline{b}}_1. \end{aligned} \quad (\text{A.7})$$

Therefore  $\underline{a}_2$  equals to zero *iff* the right hand side of (A.7) is equal to zero.

$$\underline{a}_1 = (B_1 B_1' + \Theta_1)^{-1}(B_1 \alpha - B_1 B_2' \tilde{\underline{a}}_2) \quad (\text{A.8})$$

Substituting (A.5) into (A.6) yields:

$$\begin{aligned} & [(B_2 B_2' + \Theta_2) - B_2 B_1' (B_1 B_1' + \Theta_1)^{-1} B_1 B_2'] \underline{a}_2 \\ &= B_2 [I_K - B_1' (B_1 B_1' + \Theta_1)^{-1} B_1] \\ &= B_2 (B_1' \Theta_1^{-1} B_1 + I_K)^{-1} \tilde{\underline{b}}_1 \end{aligned} \quad (\text{A.9})$$

## APPENDIX B

In this appendix we present the predictions of Hong Kong's real economic growth rate had there been no change in sovereignty or no CEPA implementation with Mainland China using the factor approach. IC1 and IC2 are used to estimate the number of underlying common factors with maximum number of  $K$  equal to 20. Both methods give  $K = 20$ , and therefore same predicted path. Tables B1 and B2 present the estimated treatment effects of political and economic integration based on Bai and Ng (2002) the IC criterion of selecting  $K$ . Figures B1 - B4 plot the within sample and post-sample predictions under political and economic integration. As one can see from these figures, both the within and post-sample predictions are a lot more volatile than using the observed data. The estimated treatment effects fitting an AR(1) model is 4.63% and is statistically significant with  $t$ -statistic equal to 8.9.

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**Table 1.1 Optimal Choice of m and the Average PMSE, 2 Stationary Factors**

T <sub>1</sub> = 25 T = 35									
	$\sigma^2=1$			$\sigma^2=0.5$			$\sigma^2=0.1$		
	AIC	AICC	20	AIC	AICC	20	AIC	AICC	20
Avg. #	11.726	4.432	-	11.418	4.468	-	11.39	4.664	-
Avg. R <sup>2</sup>	0.9291	0.8412	0.9498	0.9436	0.881	0.9597	0.986	0.9699	0.9901
Avg. PMSE	6.1888	2.3592	7.9999	2.8749	1.2214	3.7846	0.6227	0.2434	0.8875
T <sub>1</sub> = 40 T = 50									
Avg. #	6.872	4.684	-	6.924	4.794	-	7.096	4.73	-
Avg. R <sup>2</sup>	0.8175	0.7937	0.8531	0.8804	0.8644	0.904	0.9617	0.9563	0.9693
Avg. PMSE	1.8227	1.67	2.1695	0.9195	0.8492	1.0977	0.1903	0.1737	0.2197
T <sub>1</sub> = 60 T = 70									
Avg. #	6.236	5.098	-	6.266	5.056	-	6.206	5.108	-
Avg. R <sup>2</sup>	0.7711	0.7607	0.8014	0.8549	0.8484	0.8738	0.9531	0.9516	0.9592
Avg. PMSE	1.4242	1.3901	1.5422	0.7205	0.7152	0.7781	0.1459	0.1425	0.1587

**Table 1.2 Frequency Distribution of Optimal Number of m, 2 Stationary Factors**

T <sub>1</sub> = 25 T = 35							T <sub>1</sub> = 40 T = 50						T <sub>1</sub> = 60 T = 70					
	$\sigma^2=1$		$\sigma^2=0.5$		$\sigma^2=0.1$		$\sigma^2=1$		$\sigma^2=0.5$		$\sigma^2=0.1$		$\sigma^2=1$		$\sigma^2=0.5$		$\sigma^2=0.1$	
	A	B	A	B	A	B	A	B	A	B	A	B	A	B	A	B	A	B
1	1	12	1	14	0	2	5	10	0	4	1	6	3	4	1	5	0	0
2	4	59	3	55	5	47	13	34	8	36	8	30	14	31	10	23	7	16
3	9	103	4	89	15	104	23	81	22	82	20	75	28	61	38	64	35	60
4	17	107	16	112	11	109	44	122	42	110	49	125	59	95	50	105	69	110
5	14	81	15	96	18	90	72	97	77	113	79	120	88	120	88	112	89	126
6	17	73	21	65	27	65	82	86	104	73	65	74	96	91	98	95	84	94
7	28	33	37	42	33	43	77	41	66	41	71	42	86	45	81	56	88	60
8	25	19	26	19	29	25	62	20	56	29	57	17	56	29	64	24	55	20
9	34	7	47	3	29	7	46	5	47	10	54	10	34	18	35	10	43	12
10	37	6	40	3	46	5	28	4	30	0	45	1	15	2	19	5	19	2
11	36	0	44	2	29	2	20	0	25	1	27	0	10	3	8	1	6	0
12	45	0	43	0	41	1	17	0	13	1	10	0	9	1	6	0	5	0
13	46	0	35	0	37	0	6	0	4	0	12	0	1	0	2	0	0	0
14	39	0	37	0	44	0	2	0	3	0	2	0	1	0	0	0	0	0
15	45	0	44	0	38	0	1	0	3	0	0	0	0	0	0	0	0	0
16	35	0	28	0	39	0	1	0	0	0	0	0	0	0	0	0	0	0
17	38	0	23	0	30	0	0	0	0	0	0	0	0	0	0	0	0	0
18	18	0	23	0	8	0	1	0	0	0	0	0	0	0	0	0	0	0
19	10	0	11	0	16	0	0	0	0	0	0	0	0	0	0	0	0	0
20	2	0	2	0	5	0	0	0	0	0	0	0	0	0	0	0	0	0

A = AIC; B = AICC;



**Table 2.1 Optimal Choice of m and the Average PMSE, 3 Stationary Factors**

$T_1 = 25 \ T = 35$									
	$\sigma^2=1$			$\sigma^2=0.5$			$\sigma^2=0.1$		
	AIC	AICC	20	AIC	AICC	20	AIC	AICC	20
Avg. #	11.19	4.438	-	11.696	4.58	-	11.704	4.738	-
Avg. $R^2$	0.9312	0.8601	0.9524	0.9587	0.9137	0.9705	0.9884	0.9737	0.9914
Avg. PMSE	6.0833	2.3475	8.3017	3.0528	1.243	4.1386	0.6458	0.2469	0.8117
$T_1 = 40 \ T = 50$									
Avg. #	6.692	4.614	-	7.01	4.714	-	7.05	4.834	-
Avg. $R^2$	0.8563	0.8368	0.8837	0.917	0.9048	0.933	0.9754	0.9716	0.9801
Avg. PMSE	1.8804	1.7127	2.2374	0.9663	0.874	1.1342	0.1857	0.1652	0.221
$T_1 = 60 \ T = 70$									
Avg. #	6.114	4.922	-	6.172	5.004	-	6.262	5.104	-
Avg. $R^2$	0.8255	0.8183	0.8485	0.8861	0.8809	0.9009	0.9679	0.9668	0.9721
Avg. PMSE	1.3887	1.3565	1.5384	0.7115	0.6971	0.7841	0.1397	0.1389	0.1552

**Table 2.2 Frequency Distribution of Optimal Number of m, 3 Stationary Factors**

$T_1 = 25 \ T = 35$							$T_1 = 40 \ T = 50$						$T_1 = 60 \ T = 70$					
	$\sigma^2=1$		$\sigma^2=0.5$		$\sigma^2=0.1$		$\sigma^2=1$		$\sigma^2=0.5$		$\sigma^2=0.1$		$\sigma^2=1$		$\sigma^2=0.5$		$\sigma^2=0.1$	
	A	B	A	B	A	B	A	B	A	B	A	B	A	B	A	B	A	B
1	2	17	1	10	0	3	4	13	2	4	0	1	1	1	0	3	0	0
2	5	57	2	49	1	45	9	44	12	31	12	33	15	28	12	23	16	24
3	5	100	7	104	9	94	29	77	23	88	19	71	40	68	30	69	32	61
4	15	104	10	97	17	113	68	127	44	118	55	120	67	116	67	107	64	105
5	28	85	16	101	12	94	70	91	69	111	72	114	93	115	93	118	79	110
6	24	65	22	65	18	61	75	72	75	72	68	79	73	94	94	88	83	103
7	24	36	28	34	28	42	71	42	73	48	68	59	88	43	79	54	88	58
8	31	26	34	20	31	32	58	23	56	21	68	11	48	23	54	22	60	28
9	43	6	30	13	32	8	38	9	62	6	47	8	38	9	38	14	41	8
10	43	1	35	6	38	5	31	1	38	1	41	4	22	2	19	2	23	2
11	40	3	46	0	39	2	26	1	23	0	22	0	10	1	10	0	10	1
12	43	0	45	1	42	1	12	0	14	0	16	0	3	0	4	0	3	0
13	30	0	48	0	47	0	6	0	7	0	5	0	1	0	0	0	1	0
14	43	0	36	0	56	0	1	0	1	0	3	0	1	0	0	0	0	0
15	35	0	42	0	38	0	2	0	0	0	2	0	0	0	0	0	0	0
16	32	0	35	0	27	0	0	0	1	0	2	0	0	0	0	0	0	0
17	31	0	33	0	37	0	0	0	0	0	0	0	0	0	0	0	0	0
18	17	0	16	0	19	0	0	0	0	0	0	0	0	0	0	0	0	0
19	7	0	11	0	6	0	0	0	0	0	0	0	0	0	0	0	0	0
20	2	0	3	0	3	0	0	0	0	0	0	0	0	0	0	0	0	0

A = AIC; B = AICC;

**Table 3.1 Optimal Choice of m and the Average PMSE, i.i.d. Factor**

$T_1 = 25 \quad T = 35$									
	$\sigma^2=1$			$\sigma^2=0.5$			$\sigma^2=0.1$		
	AIC	AICC	20	AIC	AICC	20	AIC	AICC	20
Avg. #	11.614	4.92	-	11.738	5.03	-	11.904	4.972	-
Avg. $R^2$	0.9389	0.8714	0.9555	0.9657	0.9266	0.9759	0.99	0.9782	0.9929
Avg. PMSE	5.9299	2.601	8.0873	3.3748	1.3028	4.3716	0.6594	0.2617	0.8572
$T_1 = 40 \quad T = 50$									
Avg. #	6.174	3.99	-	6.474	4.184	-	6.224	4.05	-
Avg. $R^2$	0.6729	0.6306	0.7402	0.7291	0.6883	0.7835	0.8651	0.8469	0.8932
Avg. PMSE	1.6635	1.4858	2.0566	0.8903	0.7674	1.0975	0.1696	0.1501	0.2107
$T_1 = 60 \quad T = 70$									
Avg. #	6.82	5.61	-	7.016	5.744	-	7.19	5.868	-
Avg. $R^2$	0.8182	0.8101	0.8397	0.8919	0.8872	0.9048	0.9752	0.974	0.9781
Avg. PMSE	1.5597	1.5375	1.6305	0.8022	0.7854	0.8393	0.1590	0.156	0.1655

**Table 3.2 Frequency Distribution of Optimal Number of m, i.i.d. Factor**

$T_1 = 25 \quad T = 35$							$T_1 = 40 \quad T = 50$						$T_1 = 60 \quad T = 70$					
	$\sigma^2=1$		$\sigma^2=0.5$		$\sigma^2=0.1$		$\sigma^2=1$		$\sigma^2=0.5$		$\sigma^2=0.1$		$\sigma^2=1$		$\sigma^2=0.5$		$\sigma^2=0.1$	
	A	B	A	B	A	B	A	B	A	B	A	B	A	B	A	B	A	B
1	0	4	1	3	0	0	8	26	8	27	9	21	1	3	0	0	0	0
2	5	33	1	20	2	21	33	77	23	67	25	72	5	10	4	6	0	3
3	3	73	6	77	5	76	50	113	35	104	36	95	18	34	12	28	12	27
4	11	121	10	110	8	134	63	104	65	108	66	128	38	75	35	80	23	62
5	13	104	18	110	19	98	72	84	68	80	71	95	67	112	67	123	55	114
6	18	69	23	81	22	72	73	58	73	56	82	51	94	126	89	109	111	134
7	35	49	32	49	29	55	54	23	71	33	65	25	103	78	106	88	99	90
8	24	26	22	34	19	32	44	9	42	14	47	10	77	44	74	35	87	45
9	42	13	37	12	29	5	28	3	37	7	41	3	46	14	54	23	45	16
10	37	5	52	2	48	5	36	1	30	2	27	0	30	4	33	5	36	8
11	41	2	35	2	40	2	18	2	24	0	15	0	13	0	16	2	18	1
12	50	0	45	0	47	0	11	0	12	1	11	0	5	0	3	1	10	0
13	59	1	34	0	46	0	6	0	6	1	3	0	2	0	6	0	3	0
14	46	0	41	0	44	0	1	0	4	0	2	0	1	0	0	0	0	0
15	37	0	42	0	36	0	1	0	0	0	0	0	0	0	1	0	1	0
16	27	0	33	0	35	0	0	0	2	0	0	0	0	0	0	0	0	0
17	18	0	22	0	32	0	2	0	0	0	0	0	0	0	0	0	0	0
18	18	0	25	0	27	0	0	0	0	0	0	0	0	0	0	0	0	0
19	13	0	16	0	10	0	0	0	0	0	0	0	0	0	0	0	0	0
20	3	0	5	0	2	0	0	0	0	0	0	0	0	0	0	0	0	0

A = AIC; B = AICC;

**Table 4.1 Optimal Choice of m and the Average PMSE, Nearly Non-stationary Factor**

$T_1 = 25 \ T = 35$									
	$\sigma^2=1$			$\sigma^2=0.5$			$\sigma^2=0.1$		
	AIC	AICC	20	AIC	AICC	20	AIC	AICC	20
Avg. #	11.692	4.28	-	11.728	4.156	-	11.452	4.206	-
Avg. $R^2$	0.9123	0.8048	0.9374	0.9305	0.8391	0.9504	0.962	0.9222	0.9728
Avg. PMSE	6.2022	2.2714	8.4701	3.2219	1.1118	4.1398	0.7399	0.2213	0.935
$T_1 = 40 \ T = 50$									
Avg. #	6.358	4.16	-	6.342	4.114	-	6.488	4.214	-
Avg. $R^2$	0.7955	0.7696	0.8378	0.8528	0.8332	0.8827	0.9237	0.9147	0.9393
Avg. PMSE	1.7769	1.6214	2.1585	0.851	0.7574	1.0292	0.1786	0.156	0.2124
$T_1 = 60 \ T = 70$									
Avg. #	5.468	4.308	-	5.432	4.302	-	5.472	4.272	-
Avg. $R^2$	0.77	0.7602	0.8019	0.8239	0.8159	0.8476	0.9139	0.9101	0.9259
Avg. PMSE	1.3278	1.2805	1.4846	0.6737	0.6517	0.7699	0.1286	0.125	0.1457

**Table 4.2 Frequency Distribution of Optimal Number of m, Nearly Non-stationary Factor**

$T_1 = 25 \ T = 35$							$T_1 = 40 \ T = 50$						$T_1 = 60 \ T = 70$					
	$\sigma^2=1$		$\sigma^2=0.5$		$\sigma^2=0.1$		$\sigma^2=1$		$\sigma^2=0.5$		$\sigma^2=0.1$		$\sigma^2=1$		$\sigma^2=0.5$		$\sigma^2=0.1$	
	A	B	A	B	A	B	A	B	A	B	A	B	A	B	A	B	A	B
1	0	25	2	32	3	25	4	22	2	19	6	15	11	17	6	11	8	20
2	3	73	7	72	7	74	28	75	30	72	22	73	30	55	40	65	24	56
3	12	99	12	101	5	99	47	99	39	98	41	94	53	101	58	102	75	94
4	9	106	11	103	16	102	57	105	64	130	52	124	87	113	70	116	75	115
5	22	78	12	73	24	86	65	84	80	77	76	95	90	100	86	91	87	106
6	25	41	24	62	31	56	74	63	71	59	72	42	81	58	96	56	79	65
7	25	39	19	24	19	26	66	32	58	26	67	32	56	30	56	33	68	21
8	33	23	36	19	33	18	51	13	51	13	51	15	39	20	43	19	32	15
9	27	8	39	11	31	10	33	5	42	5	38	6	31	6	24	5	26	5
10	22	6	32	2	44	2	35	2	24	1	37	2	12	0	15	1	14	3
11	48	1	37	1	33	1	24	0	14	0	14	1	6	0	4	1	7	0
12	40	1	32	0	34	1	11	0	11	0	8	1	2	0	2	0	3	0
13	44	0	47	0	36	0	3	0	6	0	12	0	1	0	0	0	1	0
14	40	0	40	0	38	0	1	0	6	0	4	0	1	0	0	0	1	0
15	46	0	43	0	40	0	1	0	2	0	0	0	0	0	0	0	0	0
16	39	0	34	0	33	0	0	0	0	0	0	0	0	0	0	0	0	0
17	35	0	28	0	31	0	0	0	0	0	0	0	0	0	0	0	0	0
18	16	0	17	0	22	0	0	0	0	0	0	0	0	0	0	0	0	0
19	11	0	21	0	14	0	0	0	0	0	0	0	0	0	0	0	0	0
20	3	0	7	0	6	0	0	0	0	0	0	0	0	0	0	0	0	0

A = AIC; B = AICC;

**Table 5. Prediction comparison of model with****N=20, T<sub>0</sub>=25, T=35, K=1, F~N(0,1), B~N(0,1), kmax=8, σ=1**

	<b>R<sup>2</sup></b>	<b>PMSE</b>	<b>Average number of Regressors</b>
AIC	0.8246	5.5135	11.092
AICC	0.6386	2.0310	4.034
PC1	0.5245	1.5724	7.880
PC2	0.4992	1.4896	7.012
PC3	0.5278	1.5799	8
IC1	0.3346	1.1108	1.356
IC2	0.3262	1.0767	1.002
IC3	0.5278	1.5799	8

**Table 6. Prediction comparison of model with****N=20, T<sub>0</sub>=25, T=35, K=1, F~N(0,1), B~N(0,1), kmax=20, σ=1**

	<b>R<sup>2</sup></b>	<b>PMSE</b>	<b>Average number of Regressors</b>
AIC	0.8396	5.6705	11.392
AICC	0.6497	2.0088	4.112
PC1	0.8882	7.9356	20
PC2	0.8882	7.9356	20
PC3	0.8882	7.9356	20
IC1	0.8882	7.9356	20
IC2	0.8882	7.9356	20
IC3	0.8882	7.9356	20

**Table 7. Prediction comparison of model with****N=20, T<sub>0</sub>=25, T=35, K=5, F~N(0,1), B~N(0,1), kmax=20, σ=1**

	<b>R<sup>2</sup></b>	<b>PMSE</b>	<b>Average number of Regressors</b>
AIC	0.9349	7.2288	12.1520
AICC	0.8584	3.3378	5.366
PC1	0.9527	9.2582	20
PC2	0.9527	9.2582	20
PC3	0.9527	9.2582	20
IC1	0.9527	9.2582	20
IC2	0.9527	9.2582	20
IC3	0.9527	9.2582	20

**Table 8. Prediction comparison of model with****N=20, T<sub>0</sub>=25, T=35, K=5, F~N(0,1), B~U(-1,1), kmax=20, σ=1**

	<b>R<sup>2</sup></b>	<b>PMSE</b>	<b>Average number of Regressors</b>
AIC	0.8820	7.8766	11.98
AICC	0.7355	2.8996	4.864
PC1	0.9147	9.9083	20
PC2	0.9147	9.9083	20
PC3	0.9147	9.9083	20
IC1	0.9147	9.9083	20
IC2	0.9147	9.9083	20
IC3	0.9147	9.9083	20

**Table 9. Prediction comparison of model with****N=20, T<sub>0</sub>=25, T=35, K=5, F~N(0,1), B~N(0.3,1), kmax=20, σ=1**

	<b>R<sup>2</sup></b>	<b>PMSE</b>	<b>Average number of Regressors</b>
AIC	0.9386	8.5870	12.018
AICC	0.8655	3.0519	5.162
PC1	0.9549	11.6829	20
PC2	0.9549	11.6829	20
PC3	0.9549	11.6829	20
IC1	0.9549	11.6829	20
IC2	0.9549	11.6829	20
IC3	0.9549	11.6829	20

**Table 10. Prediction comparison of model with****N=20, T<sub>0</sub>=25, T=35, K=5, F~N(0,1), B~N(1,1), kmax=20, σ=1**

	<b>R<sup>2</sup></b>	<b>PMSE</b>	<b>Average number of Regressors</b>
AIC	0.9590	8.4321	12.296
AICC	0.9074	3.7535	5.524
PC1	0.9691	11.1183	20
PC2	0.9691	11.1183	20
PC3	0.9691	11.1183	20
IC1	0.9691	11.1183	20
IC2	0.9691	11.1183	20
IC3	0.9691	11.1183	20

**Table 11. Prediction comparison of model with** **$N=20, T_0=25, T=35, K=5, F \sim N(0,1), B \sim N(2,2), k_{\max}=20, \sigma=1$** 

	$R^2$	PMSE	Average number of Regressors
AIC	0.9821	9.4982	12.39
AICC	0.9612	5.0858	6.034
PC1	0.9865	11.8991	20
PC2	0.9865	11.8991	20
PC3	0.9865	11.8991	20
IC1	0.9865	11.8991	20
IC2	0.9865	11.8991	20
IC3	0.9865	11.8991	20

**Table 12. Prediction comparison of model with** **$N=20, T_0=25, T=35, K=5, F \sim N(0,1), B \sim N(0,1), k_{\max}=20, \sigma \sim U(1,4)$** 

	$R^2$	PMSE	Average number of Regressors
AIC	0.8338	41.4836	11.57
AICC	0.6382	16.4713	4.466
PC1	0.8810	55.8442	20
PC2	0.8810	55.8442	20
PC3	0.8810	55.8442	20
IC1	0.8810	55.8442	20
IC2	0.8810	55.8442	20
IC3	0.8810	55.8442	20

**Table13. Prediction comparison of model with** **$N=20, T_0=25, T=35, K=5, F \sim N(0,1), B \sim N(0,1), k_{\max}=20, e_{i,t}=0.5 \cdot e_{i,t-1} + v_{i,t}, \sigma_v=1$** 

	$R^2$	PMSE	Average number of Regressors
AIC	0.9445	10.5882	12.188
AICC	0.8779	4.3454	5.744
PC1	0.9589	13.8675	20
PC2	0.9589	13.8675	20
PC3	0.9589	13.8675	20
IC1	0.9589	13.8675	20
IC2	0.9589	13.8675	20
IC3	0.9589	13.8675	20

**Table 14. Prediction comparison of model with****N=20, T<sub>0</sub>=60, T=70, K=5, F~N(0,1), B~N(1,1), kmax=20, σ=1**

	<b>R<sup>2</sup></b>	<b>PMSE</b>	<b>Average number of Regressors</b>
AIC	0.8865	1.8256	8.024
AICC	0.8799	1.8423	6.66
PC1	0.8986	1.8789	20
PC2	0.8986	1.8789	20
PC3	0.8986	1.8789	20
IC1	0.8986	1.8789	20
IC2	0.8986	1.8789	20
IC3	0.8986	1.8789	20

**Table 15. Prediction comparison of model with****N=20, T<sub>0</sub>=25, T=35, K=5, F~N(0,1), B~N(0,1), kmax=20, σ=5**

	<b>R<sup>2</sup></b>	<b>PMSE</b>	<b>Average number of Regressors</b>
AIC	0.8510	32.0960	11.77
AICC	0.6615	13.5590	4.618
PC1	0.8919	42.9199	20
PC2	0.8919	42.9199	20
PC3	0.8919	42.9199	20
IC1	0.8919	42.9199	20
IC2	0.8919	42.9199	20
IC3	0.8919	42.9199	20

**Table 16. AICC – Weights of Control Groups for the Period 1993Q1 – 1997Q2**

	<b>Beta</b>	<b>Std</b>	<b>T</b>
Constant	0.0263	0.017	1.5427
Japan	-0.676	0.1117	-6.0522
Korea	-0.4323	0.0634	-6.8211
US	0.486	0.2195	2.2141
Taiwan	0.7926	0.3099	2.5576
R <sup>2</sup> = 0.9314; AICC = -171.771			

**Table 17. AICC – Treatment Effect of Political Integration 1997Q3 – 2003Q4**

	<b>Actual</b>	<b>Control</b>	<b>Treatment</b>
Q3-1997	0.061	0.0798	-0.0188
Q4-1997	0.014	0.081	-0.067
Q1-1998	-0.032	0.1294	-0.1614
Q2-1998	-0.061	0.1433	-0.2043
Q3-1998	-0.081	0.1319	-0.2129
Q4-1998	-0.065	0.139	-0.204
Q1-1999	-0.029	0.0876	-0.1166
Q2-1999	0.005	0.067	-0.062
Q3-1999	0.039	0.04	-0.001
Q4-1999	0.083	0.0445	0.0385
Q1-2000	0.107	0.0434	0.0636
Q2-2000	0.075	0.0398	0.0352
Q3-2000	0.076	0.0524	0.0236
Q4-2000	0.063	0.0318	0.0312
Q1-2001	0.027	0.0118	0.0152
Q2-2001	0.015	-0.0177	0.0327
Q3-2001	-0.001	-0.0177	0.0167
Q4-2001	-0.017	0.0184	-0.0354
Q1-2002	-0.01	0.0314	-0.0414
Q2-2002	0.005	0.05	-0.045
Q3-2002	0.028	0.0577	-0.0297
Q4-2002	0.048	0.0346	0.0134
Q1-2003	0.041	0.0538	-0.0128
Q2-2003	-0.009	0.0251	-0.0341
Q3-2003	0.038	0.0628	-0.0248
Q4-2003	0.047	0.0761	-0.0291
MEAN	0.018	0.0576	-0.0396
STD	0.0478	0.0429	0.0787
T	0.3761	1.3417	-0.5034



**Table 18. AIC – Weights of Control Groups for the Period 1993Q1 – 1997Q2**

	<b>Beta</b>	<b>Std</b>	<b>T</b>
Constant	0.0316	0.0164	1.9283
Japan	-0.69	0.1056	-6.5341
Korea	-0.3767	0.0688	-5.4721
US	0.8099	0.2873	2.8193
Philippines	-0.1624	0.0999	-1.6248
Taiwan	0.6189	0.311	1.9902
R <sup>2</sup> = 0.9438; AIC = -180.986			

**Table 19. AIC – Treatment Effect of Political Integration 1997Q3 – 2003Q4**

	<b>Actual</b>	<b>Control</b>	<b>Treatment</b>
Q3-1997	0.061	0.0839	-0.0229
Q4-1997	0.014	0.0811	-0.0671
Q1-1998	-0.032	0.1344	-0.1664
Q2-1998	-0.061	0.1438	-0.2048
Q3-1998	-0.081	0.1334	-0.2144
Q4-1998	-0.065	0.1472	-0.2122
Q1-1999	-0.029	0.0952	-0.1242
Q2-1999	0.005	0.0704	-0.0654
Q3-1999	0.039	0.0464	-0.0074
Q4-1999	0.083	0.0473	0.0357
Q1-2000	0.107	0.031	0.076
Q2-2000	0.075	0.0344	0.0406
Q3-2000	0.076	0.0394	0.0366
Q4-2000	0.063	0.0208	0.0422
Q1-2001	0.027	0.0155	0.0115
Q2-2001	0.015	-0.0101	0.0251
Q3-2001	-0.001	-0.0071	0.0061
Q4-2001	-0.017	0.0251	-0.0421
Q1-2002	-0.01	0.0375	-0.0475
Q2-2002	0.005	0.0473	-0.0423
Q3-2002	0.028	0.0593	-0.0313
Q4-2002	0.048	0.027	0.021
Q1-2003	0.041	0.0463	-0.0053
Q2-2003	-0.009	0.0302	-0.0392
Q3-2003	0.038	0.0593	-0.0213
Q4-2003	0.047	0.077	-0.03
MEAN	0.018	0.0583	-0.0403
STD	0.0478	0.0435	0.0815
T	0.3761	1.3393	-0.4953

**Table 20. AICC – Weights of Control Groups for the Period 1993Q1 – 2003Q4**

	<b>Beta</b>	<b>Std</b>	<b>T</b>
Constant	-0.0019	0.0037	-0.524
Austria	-1.0116	0.1682	-6.0128
Italy	-0.3177	0.1591	-1.9971
Korea	0.3447	0.0469	7.3506
Mexico	0.3129	0.051	6.1335
Norway	0.3222	0.0538	5.9912
Singapore	0.1845	0.0546	3.3812
$R^2 = 0.931$			
AICC = -378.9427			

**Table 21. AICC – Treatment Effect for Economic Integration 2004Q1 – 2008Q1**

	<b>Actual</b>	<b>Control</b>	<b>Treatment</b>
Q1-2004	0.077	0.0493	0.0277
Q2-2004	0.12	0.0686	0.0514
Q3-2004	0.066	0.0515	0.0145
Q4-2004	0.079	0.0446	0.0344
Q1-2005	0.062	0.0217	0.0403
Q2-2005	0.071	0.0177	0.0533
Q3-2005	0.081	0.0333	0.0477
Q4-2005	0.069	0.029	0.04
Q1-2006	0.09	0.0471	0.0429
Q2-2006	0.062	0.0417	0.0203
Q3-2006	0.064	0.025	0.039
Q4-2006	0.066	0.0009	0.0651
Q1-2007	0.055	-0.0101	0.0651
Q2-2007	0.062	0.0092	0.0528
Q3-2007	0.068	0.0143	0.0537
Q4-2007	0.069	0.0508	0.0182
Q1-2008	0.073	0.0538	0.0192
MEAN	0.0726	0.0323	0.0403
STD	0.0149	0.0213	0.016
T	4.8814	1.5132	2.5134

**Table 22. AIC – Weights of Control Groups for the Period 1993Q1 – 2003Q4**

	<b>Beta</b>	<b>Std</b>	<b>T</b>
Constant	-0.003	0.0042	-0.7095
Austria	-1.2949	0.2181	-5.9361
Germany	0.3552	0.233	1.5243
Italy	-0.5768	0.1781	-3.2394
Korea	0.3016	0.0587	5.1342
Mexico	0.234	0.0609	3.8395
Norway	0.2881	0.0562	5.1304
Switzerland	0.2436	0.1729	1.4092
Singapore	0.2222	0.0553	4.0155
Philippines	0.1757	0.1089	1.6127
$R^2 = 0.9433$			
AIC = -385.7498			

**Table 23. AIC – Treatment Effect for Economic Integration 2004Q1 – 2008Q1**

	<b>Actual</b>	<b>Control</b>	<b>Treatment</b>
Q1-2004	0.077	0.0559	0.0211
Q2-2004	0.12	0.0722	0.0478
Q3-2004	0.066	0.0446	0.0214
Q4-2004	0.079	0.0314	0.0476
Q1-2005	0.062	0.0121	0.0499
Q2-2005	0.071	0.0126	0.0584
Q3-2005	0.081	0.0314	0.0496
Q4-2005	0.069	0.0278	0.0412
Q1-2006	0.09	0.0436	0.0464
Q2-2006	0.062	0.0372	0.0248
Q3-2006	0.064	0.0292	0.0348
Q4-2006	0.066	0.0122	0.0538
Q1-2007	0.055	0.0051	0.0499
Q2-2007	0.062	0.0279	0.0341
Q3-2007	0.068	0.0255	0.0425
Q4-2007	0.069	0.0589	0.0101
Q1-2008	0.073	0.062	0.011
MEAN	0.0726	0.0347	0.0379
STD	0.0149	0.0193	0.0151
T	4.8814	1.7929	2.5122

Figure 1. AICC – Actual and Predicted Real GDP from 1993Q1 to 1997Q2

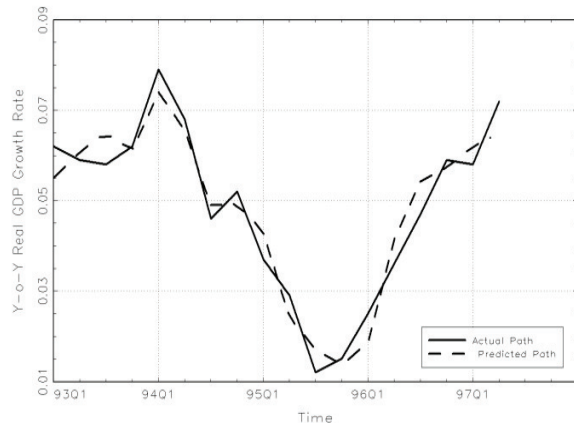


Figure 4. AIC – Actual and Predicted Real GDP from 1993Q1 to 1997Q2

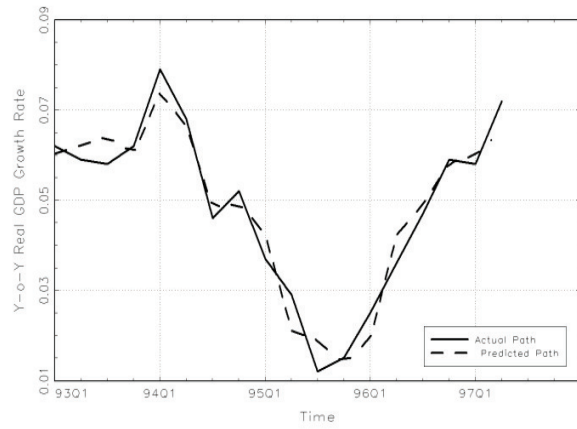


Figure 2. AICC – Actual and Counterfactual Real GDP from 1997Q3 to 2003Q4

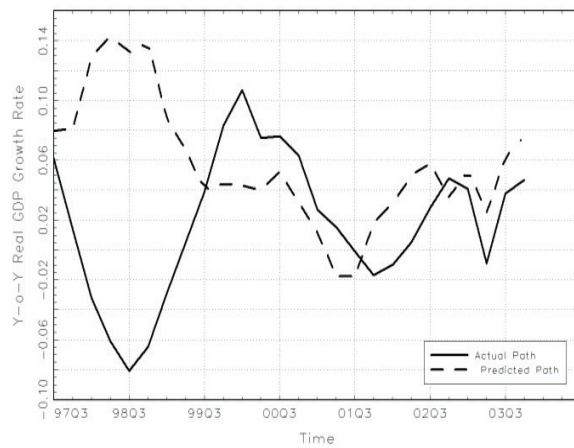


Figure 5. AIC – Actual and Counterfactual Real GDP from 1997Q3 to 2003Q4

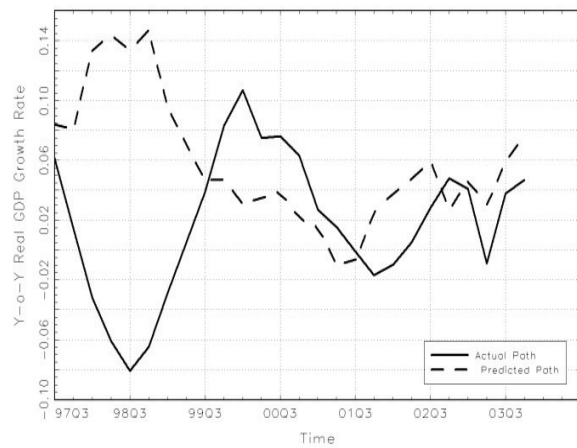


Figure 3. AICC – Autocorrelation of Treatment Effect from 1997Q3 to 2003Q4

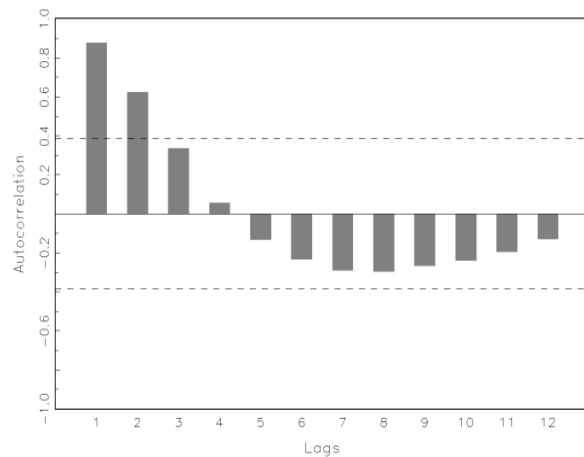


Figure 6. AIC – Autocorrelation of Treatment Effect from 1997Q3 to 2003Q4

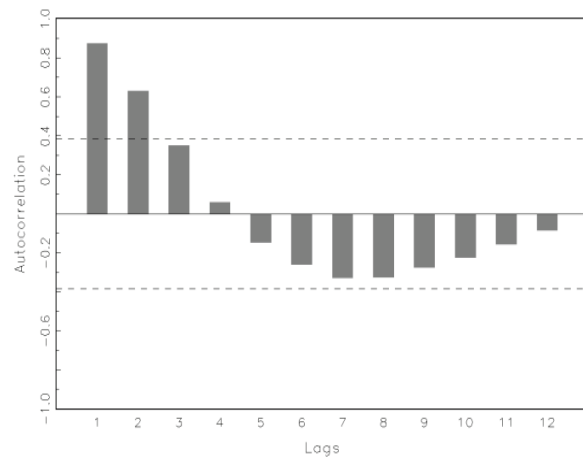


Figure 7. AICC – Actual and Predicted Real GDP from 1993Q1 to 2003Q4

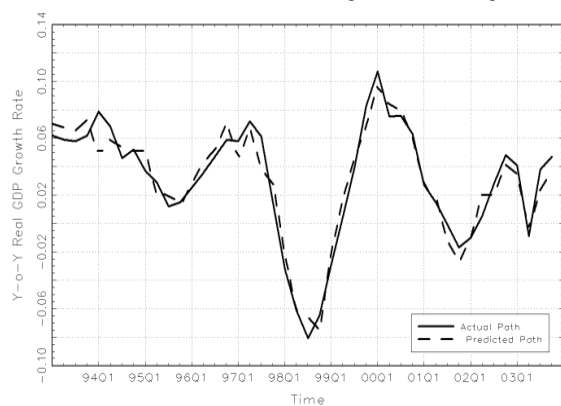


Figure 10. AIC – Actual and Predicted Real GDP from 1993Q1 to 2003Q4

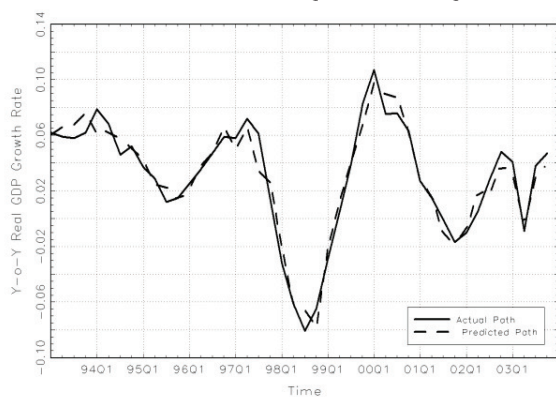


Figure 8. AICC – Actual and Counterfactual Real GDP from 2004Q1 to 2008Q1

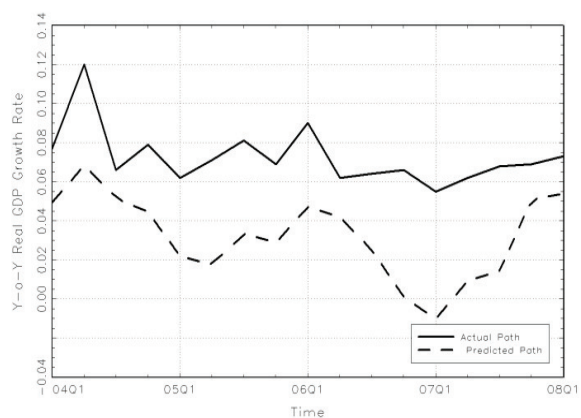


Figure 11. AIC – Actual and Counterfactual Real GDP from 2004Q1 to 2008Q1

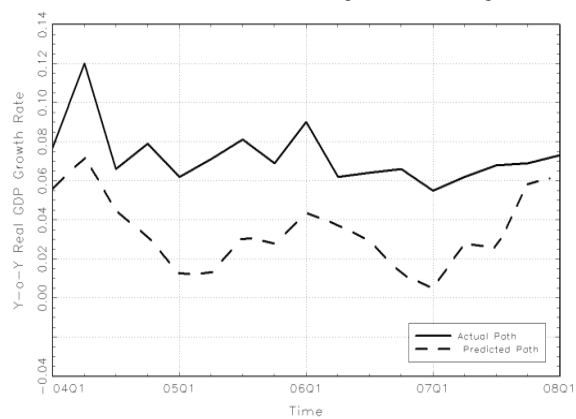


Figure 9. AICC – Autocorrelation of Treatment Effect from 2004Q1 to 2008Q1

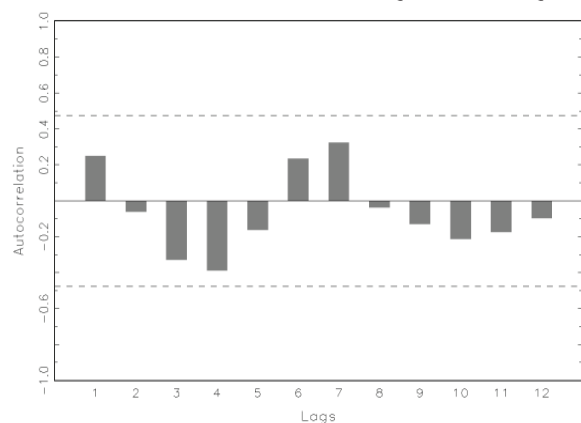


Figure 12. AIC – Autocorrelation of Treatment Effect from 2004Q1 to 2008Q1

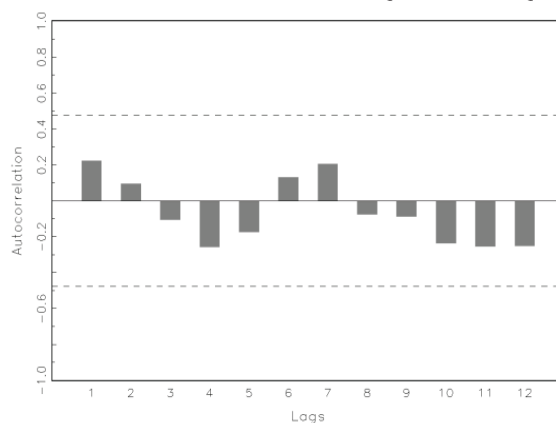


Figure B.1 Predicted Counterfactual for Political Integration from 93Q1 to 97Q2

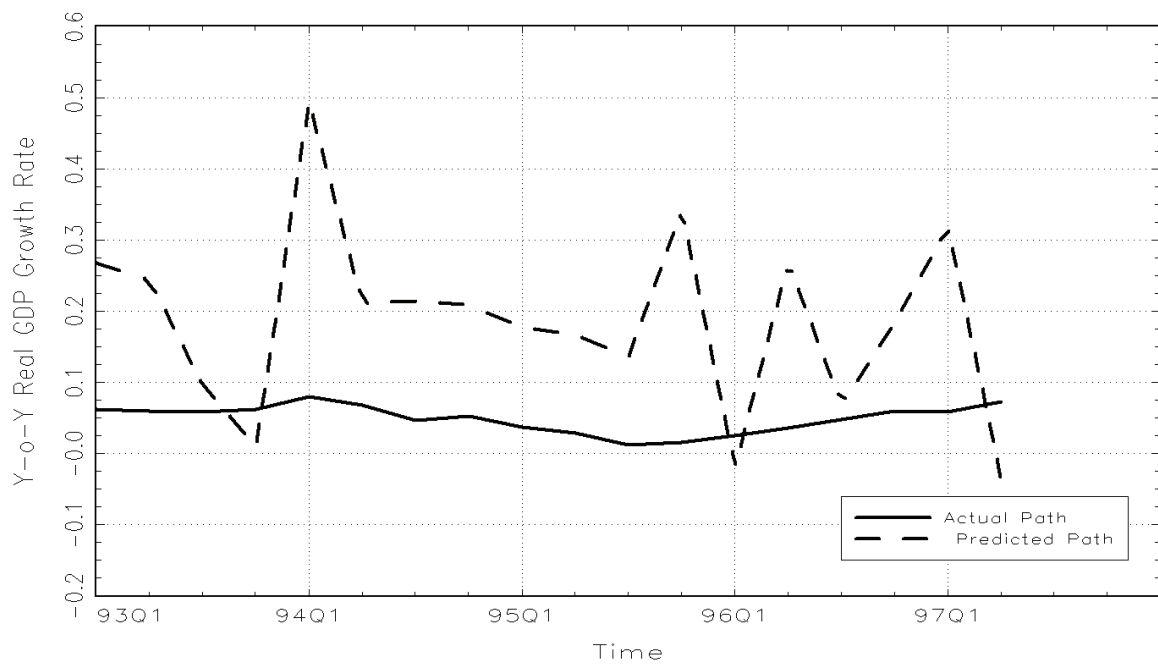


Figure B.2 Predicted Counterfactual for Political Integration from 97Q3 to 03Q4

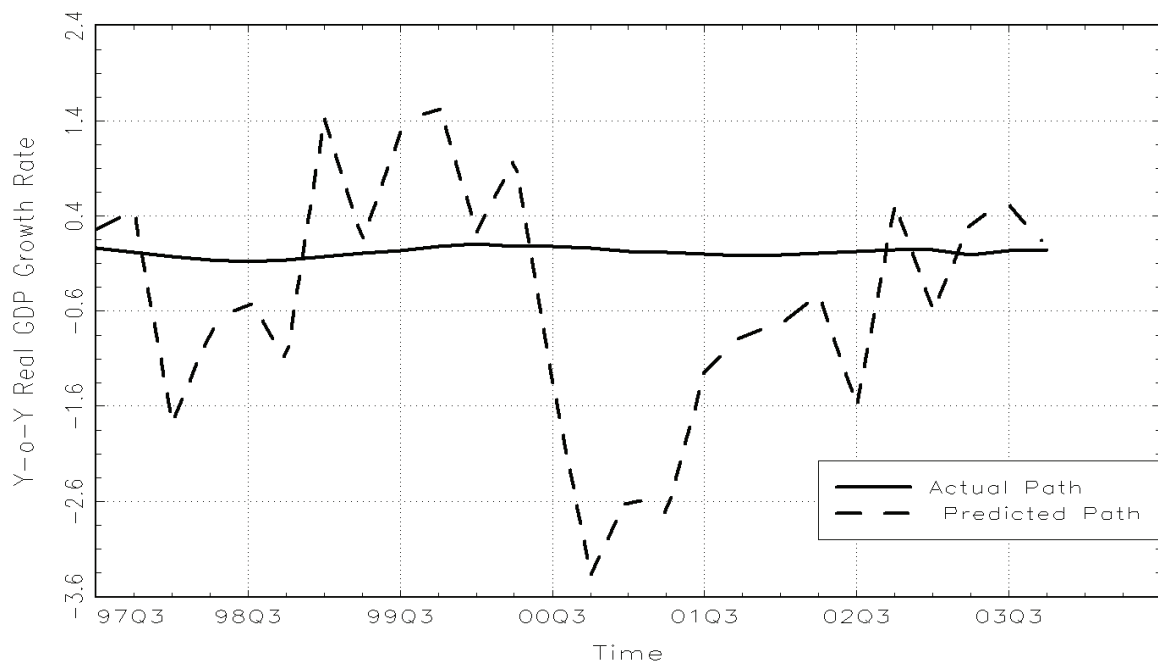
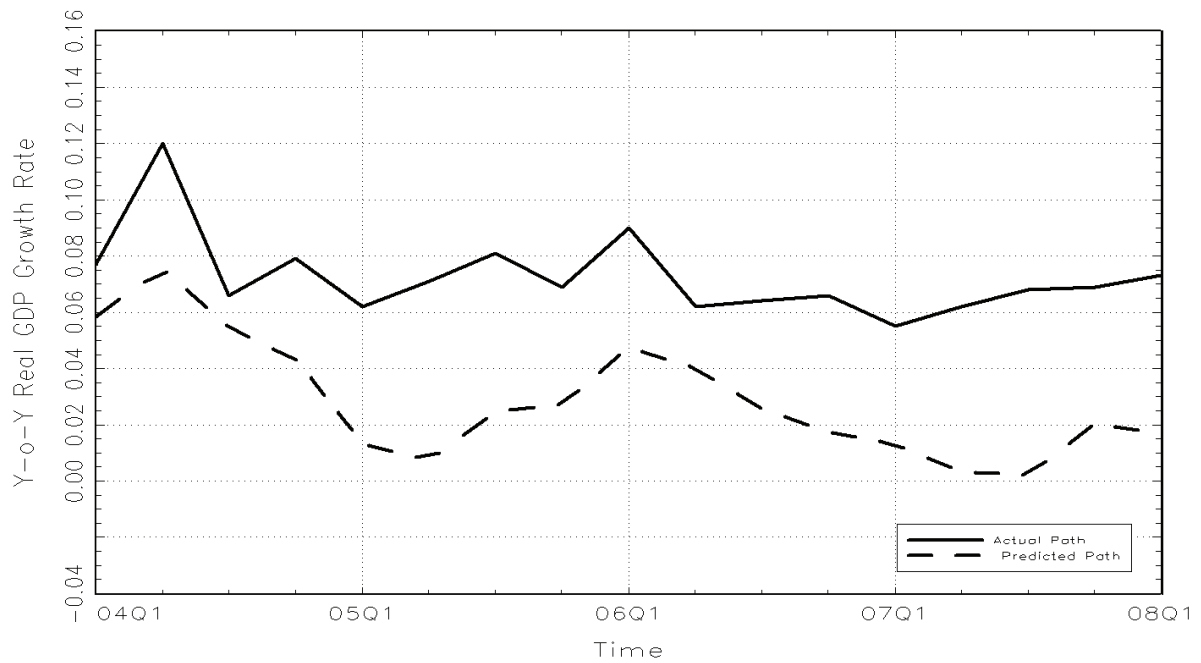


Figure B.3 Counterfactual for Economic Integration using Approximate Factor Model



Figure B.4 Counterfactual for Economic Integration using Approximate Factor Model



**Table B.1 Treatment Effect  
Political Integration<sup>1</sup>**

	<b>Actual</b>	<b>Predicted</b>	<b>Treatment</b>
97Q3	0.061	0.2526	-0.1916
97Q4	0.014	0.453	-0.439
98Q1	-0.032	-1.7748	1.7428
98Q2	-0.061	-0.8151	0.7541
98Q3	-0.081	-0.4678	0.3868
98Q4	-0.065	-1.1164	1.0514
99Q1	-0.029	1.4224	-1.4514
99Q2	0.005	0.1434	-0.1384
99Q3	0.039	1.2769	-1.2379
99Q4	0.083	1.5864	-1.5034
00Q1	0.107	0.224	-0.117
00Q2	0.075	1.0059	-0.9309
00Q3	0.076	-1.3426	1.4186
00Q4	0.063	-3.3762	3.4392
01Q1	0.027	-2.5358	2.5628
01Q2	0.015	-2.7242	2.7392
01Q3	-0.001	-1.2293	1.2283
01Q4	-0.017	-0.8478	0.8308
02Q1	-0.01	-0.7321	0.7221
02Q2	0.005	-0.4256	0.4306
02Q3	0.028	-1.5934	1.6214
02Q4	0.048	0.5178	-0.4698
03Q1	0.041	-0.5959	0.6369
03Q2	-0.009	0.357	-0.366
03Q3	0.038	0.5072	-0.4692
03Q4	0.047	0.0609	-0.0139
<b>MEAN</b>	0.018	-0.4527	0.4706
<b>STD</b>	0.0478	1.281	1.2737

**Table B.2 Treatment Effect  
Economic Integration<sup>1</sup>**

	<b>Actual</b>	<b>Predicted</b>	<b>Treatment</b>
04Q1	0.077	0.0584	0.0186
04Q2	0.12	0.0755	0.0445
04Q3	0.066	0.0545	0.0115
04Q4	0.079	0.0432	0.0358
05Q1	0.062	0.0132	0.0488
05Q2	0.071	0.0072	0.0638
05Q3	0.081	0.0248	0.0562
05Q4	0.069	0.0272	0.0418
06Q1	0.09	0.0476	0.0424
06Q2	0.062	0.0401	0.0219
06Q3	0.064	0.0258	0.0382
06Q4	0.066	0.0174	0.0486
07Q1	0.055	0.013	0.042
07Q2	0.062	0.0032	0.0588
07Q3	0.068	0.0022	0.0658
07Q4	0.069	0.0205	0.0485
08Q1	0.073	0.017	0.056
<b>MEAN</b>	0.0726	0.0289	0.0437
<b>STD</b>	0.0149	0.0211	0.0153

<sup>1</sup> IC1 gives  $\hat{K}$ =kmax=20.